

# **Manifold-constrained RNA velocity estimation with VeloCycle**

**Single Cell Transcriptomics in Python**

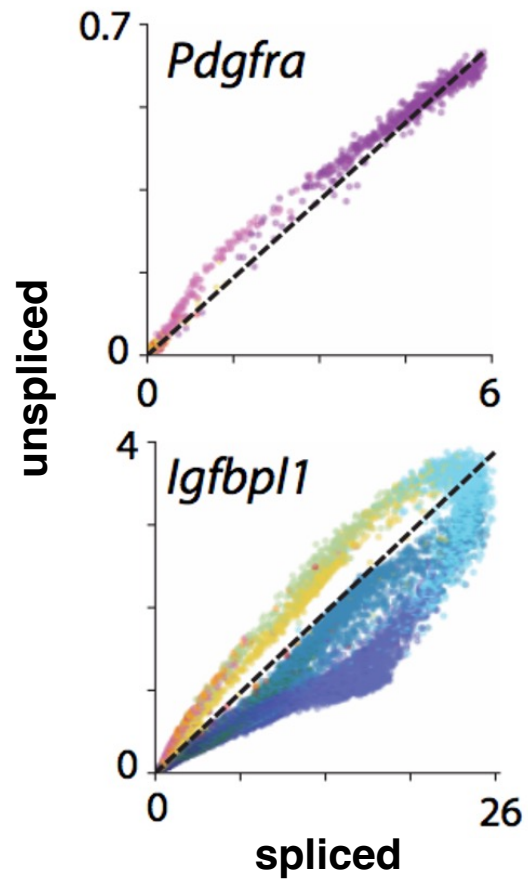
**Alex Lederer**

# Presentation Overview

- VeloCycle and probabilistic modeling
- Exercise on using VeloCycle for cycling pancreatic ductal cells

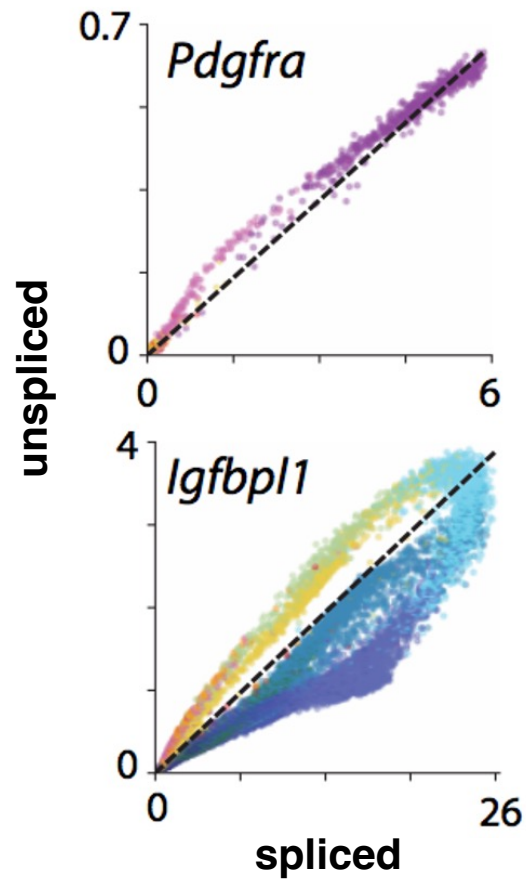
# The RNA velocity framework has several limitations

Necessity to run  
smoothing methods

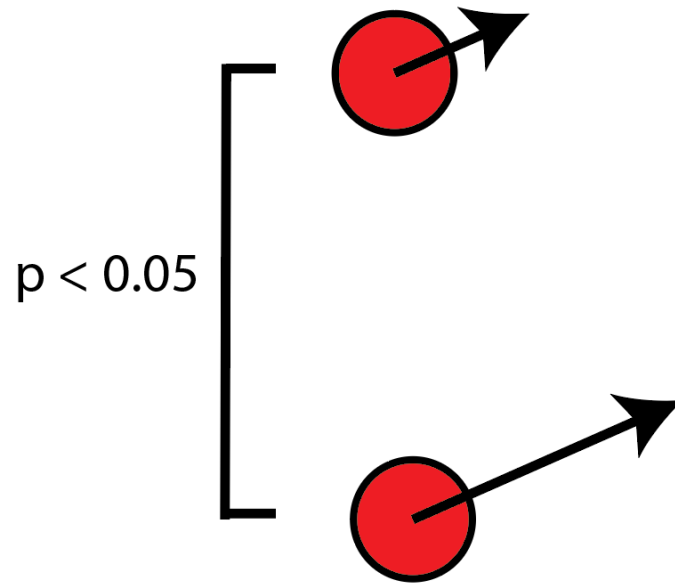


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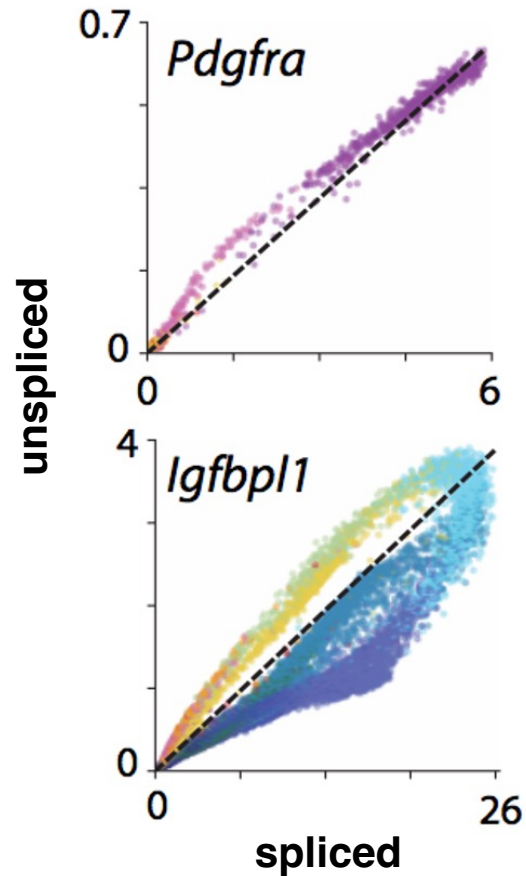


Inference on velocity is currently not possible

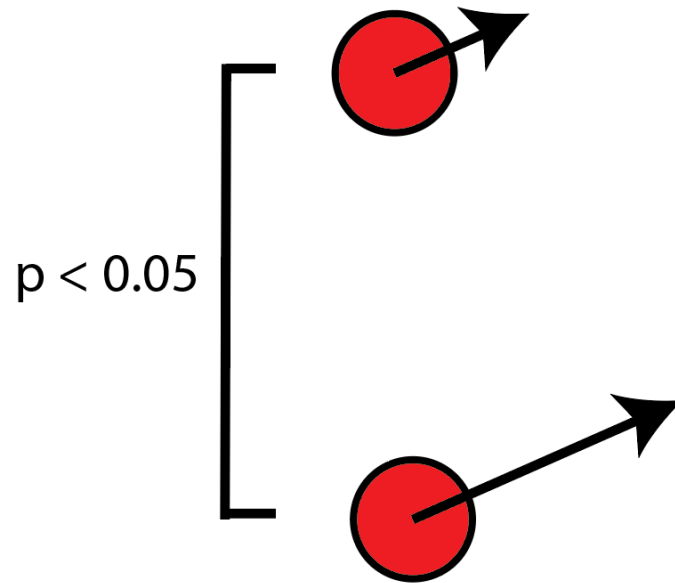


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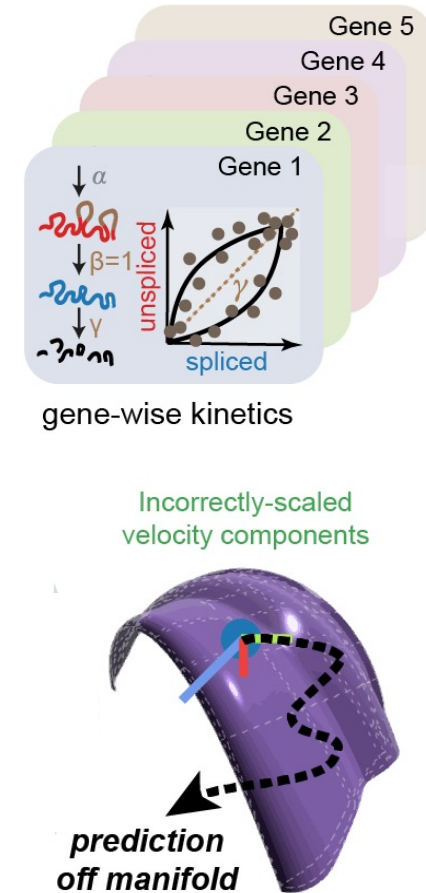
Necessity to run smoothing methods



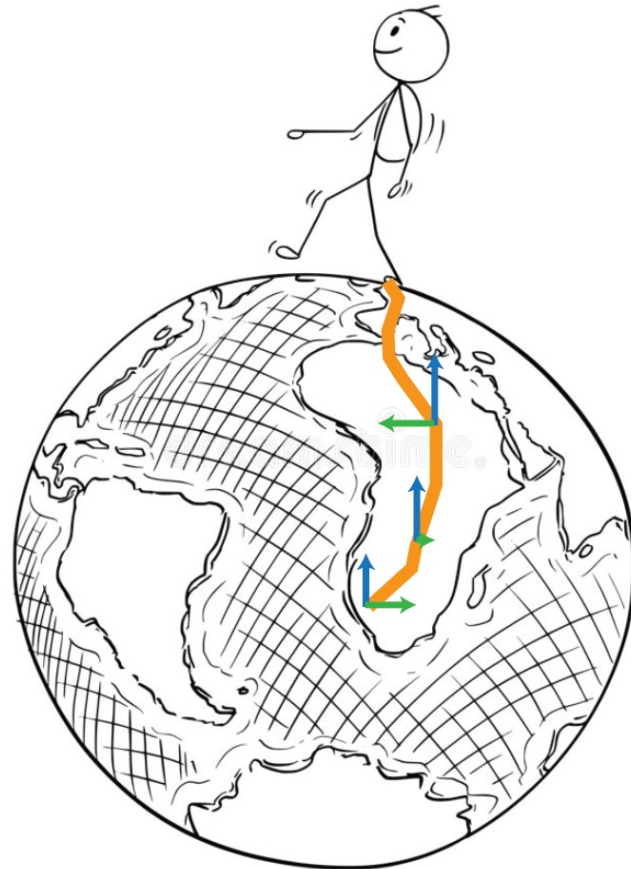
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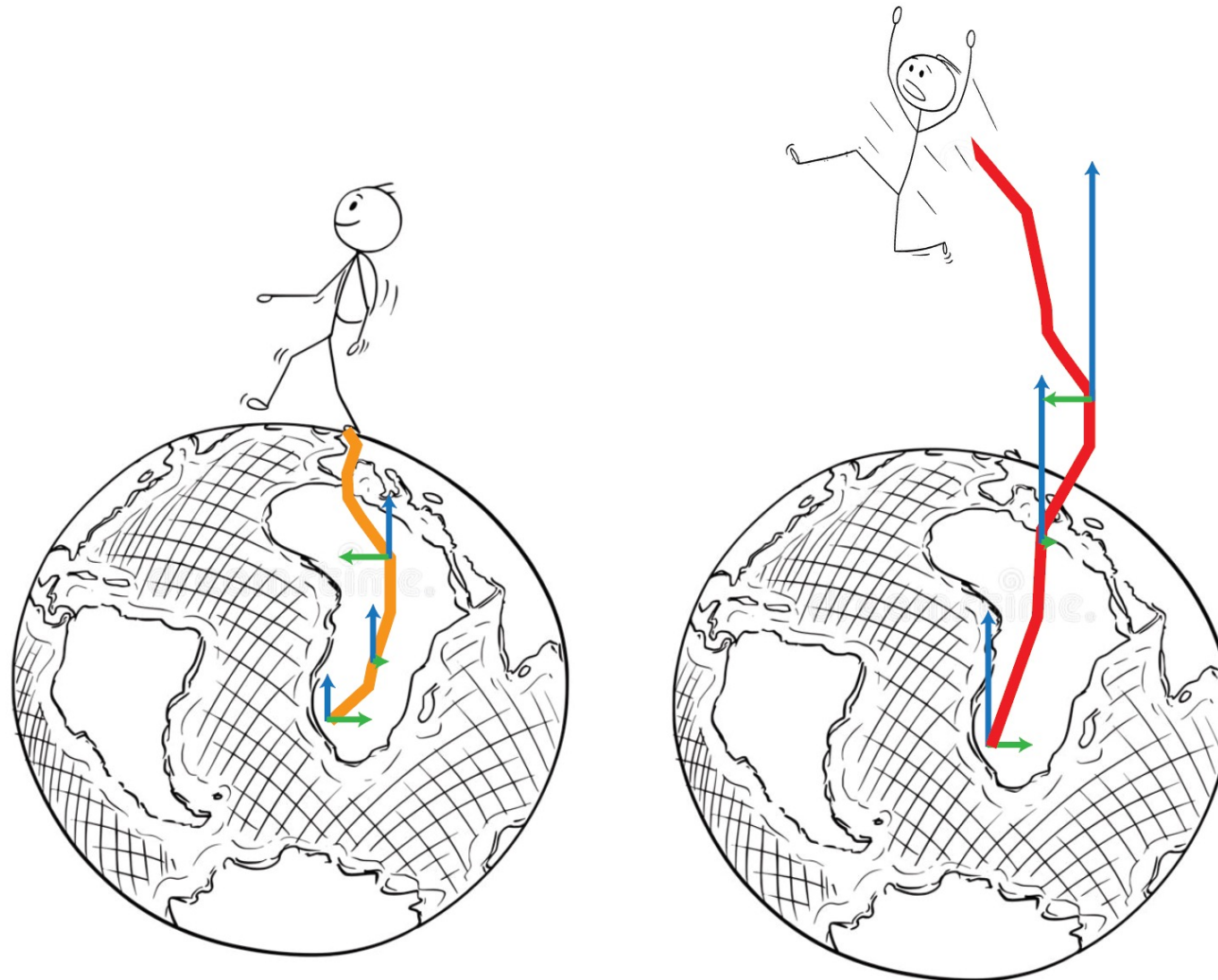
Gene-wise velocity estimates yield incorrectly scaled components



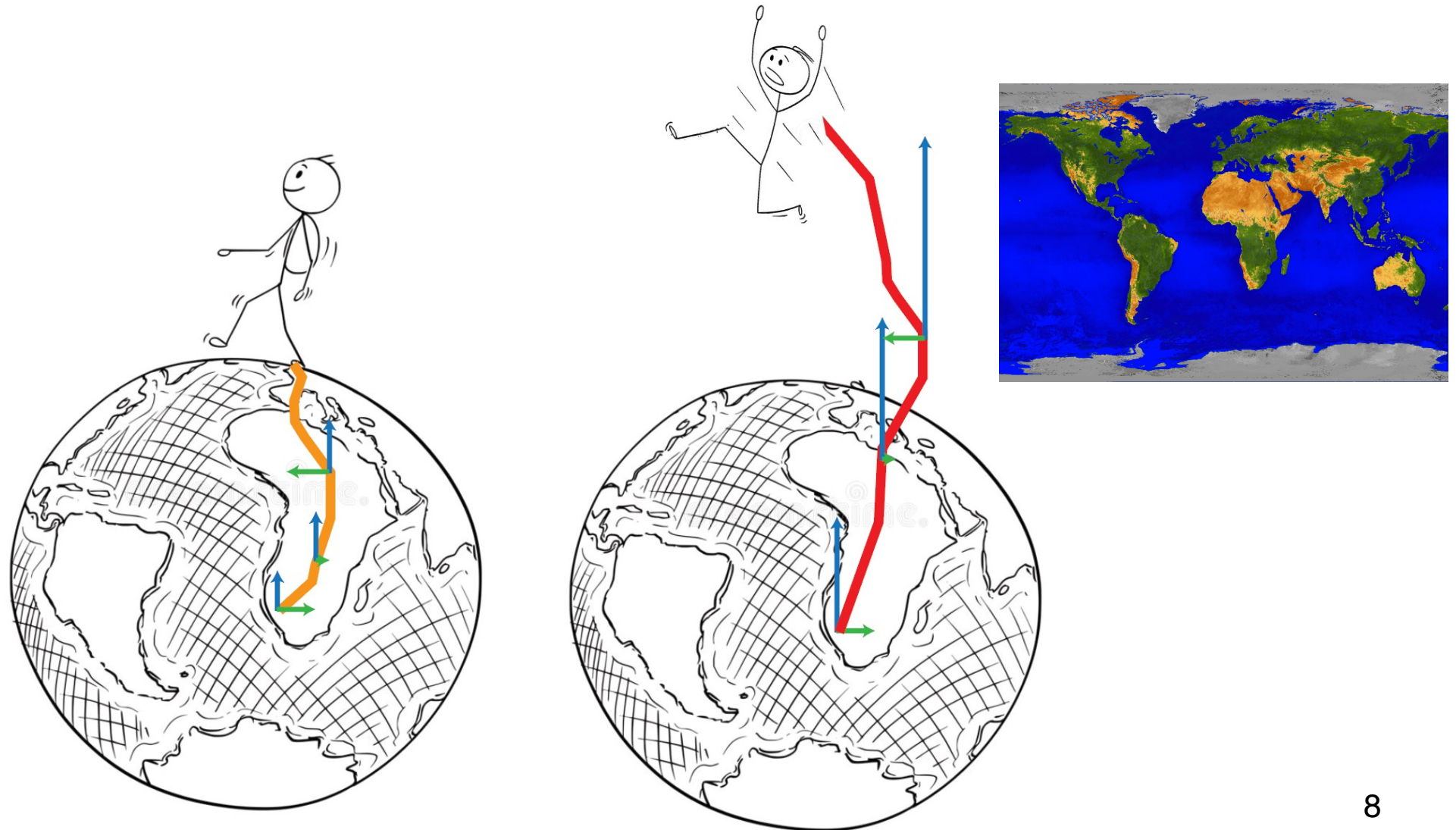
# Incorrectly scaled gene-wise velocity is not consistent to the true gene expression manifold



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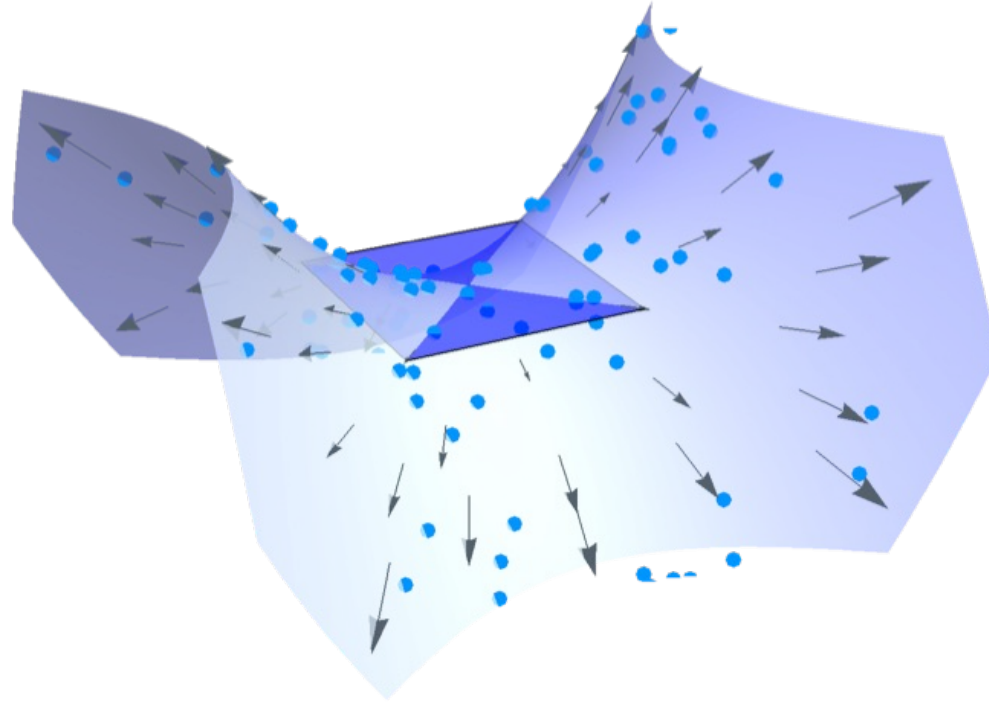


# Incorrectly scaled gene-wise velocity is not consistent to the true gene expression manifold

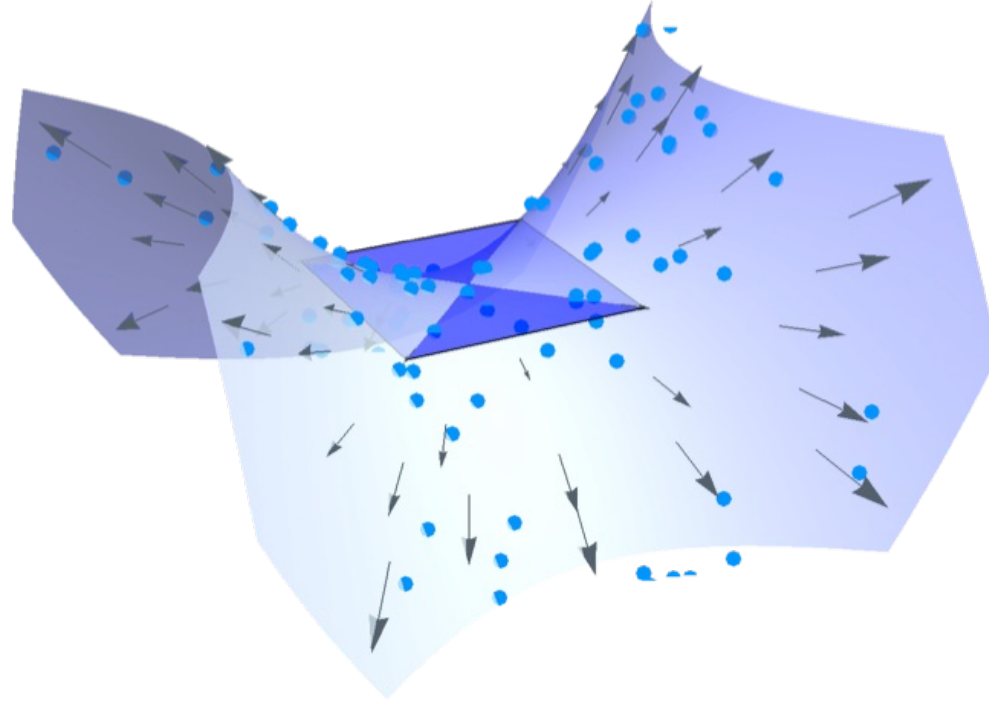




# The true gene expression manifold is high-dimensional



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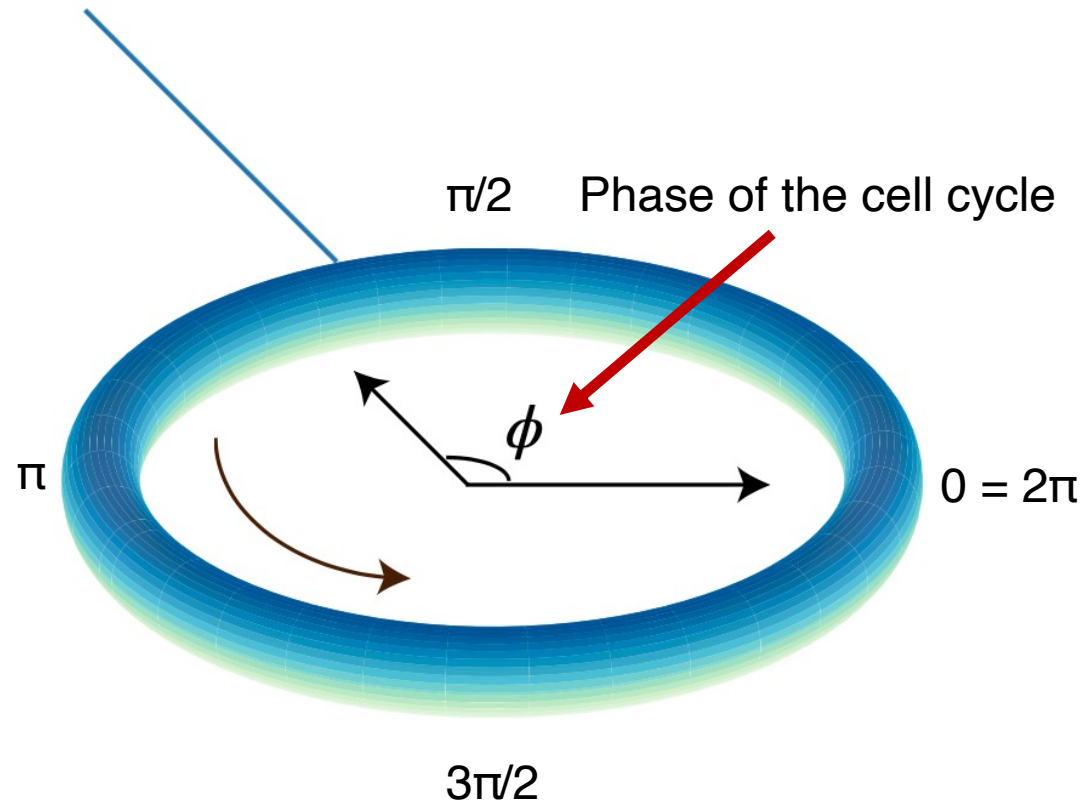


*Can we write a system of differential equations **linking** the manifold and velocity?*

*What is our true gene expression manifold?*

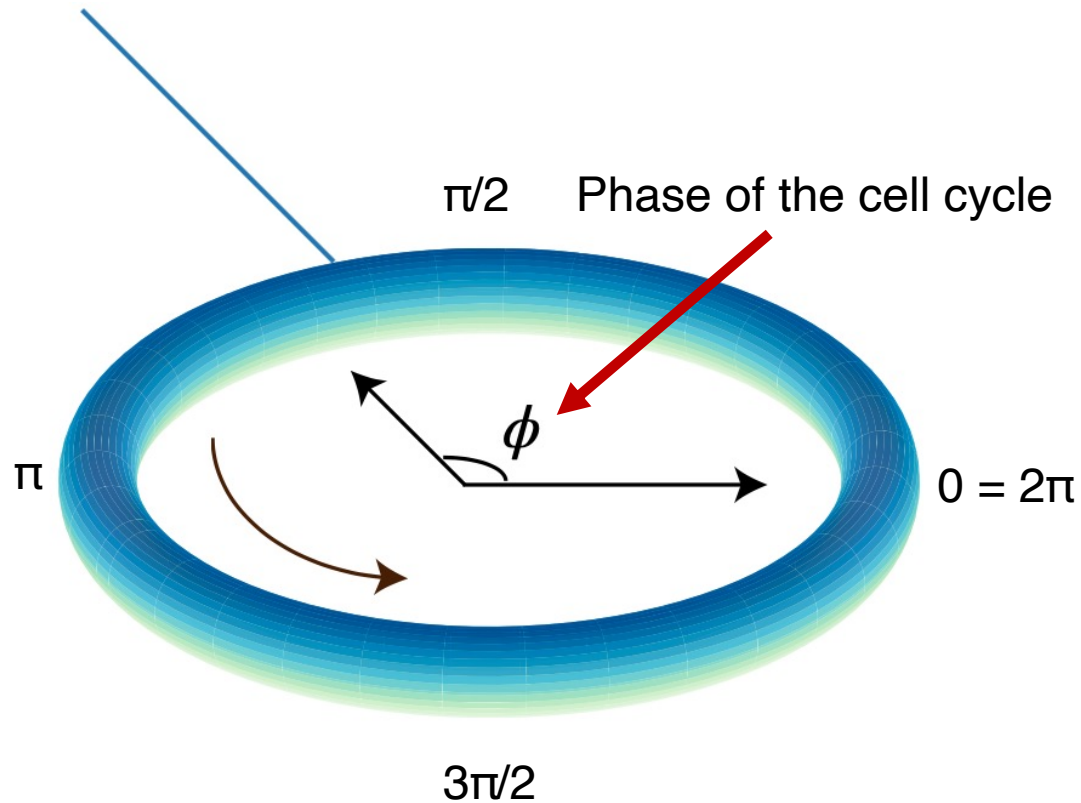
# RNA velocity can be reformulated to obtain a cell- and gene-independent cell cycle speed

1-dimensional circular manifold



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1-dimensional circular manifold



$$\frac{ds}{dt} = \beta u - \gamma s$$

becomes

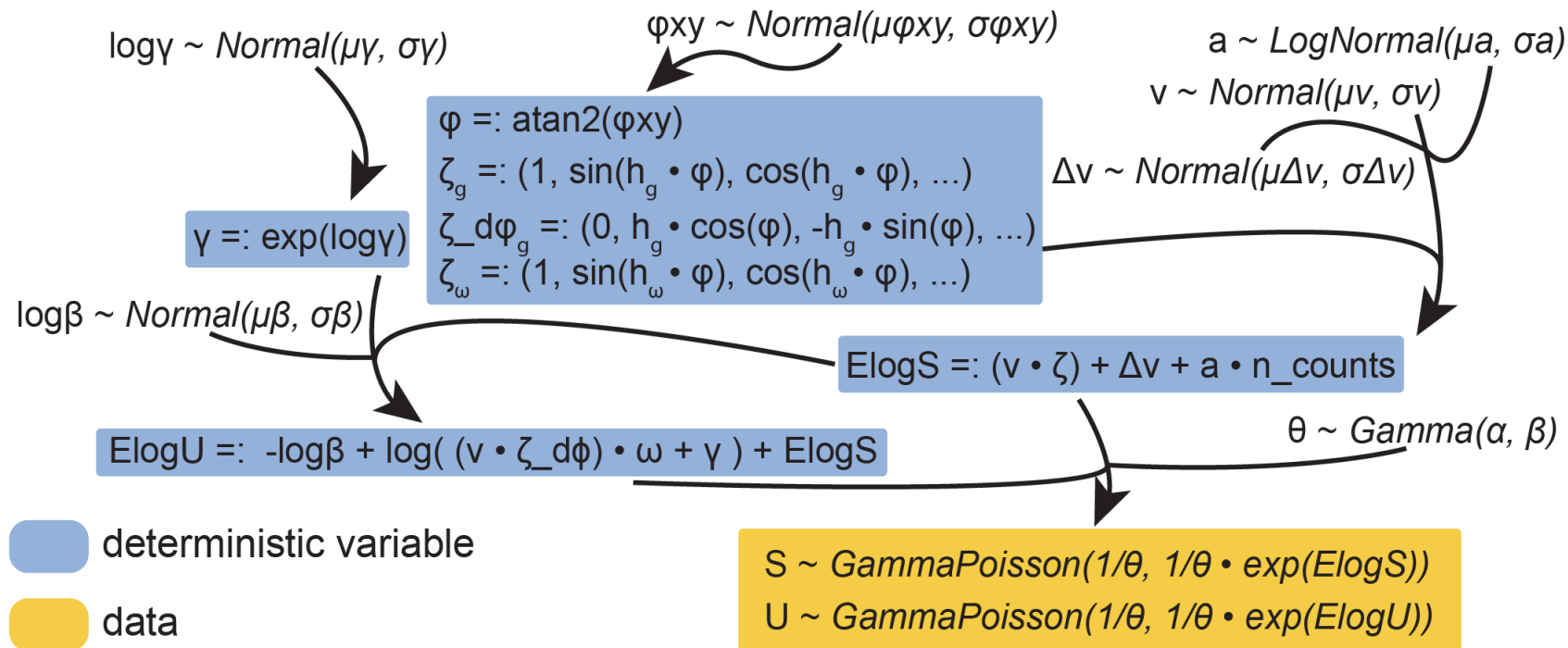
$$\nabla_{\phi} s(\phi) \cdot \omega(\phi) = \beta u(\phi) - \gamma s(\phi)$$

Speed

Phase

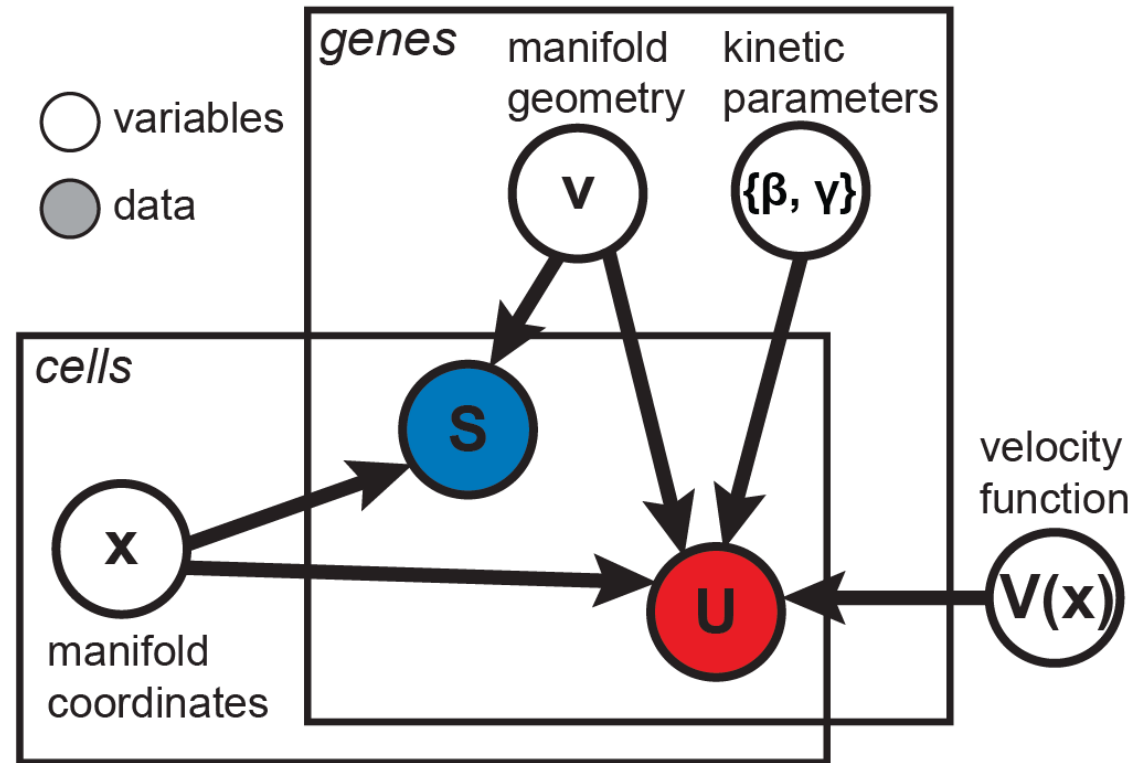
# Graphical representation of VeloCycle probabilistic model

- Each random variable is sampled from a pre-defined probability distribution
- **Bayesian inference** aims to learn the mean and variance of each variable's distribution
- Similar types of models have been developed for other single-cell challenges, including data integration and clustering.



# Graphical representation of VeloCycle probabilistic model

*Simplified graphical model*

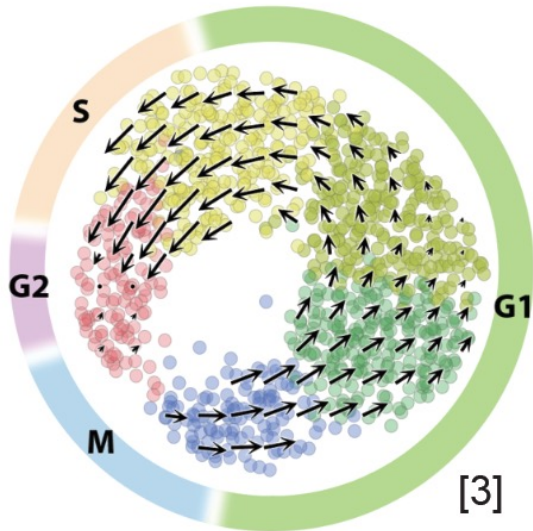


$$S \sim \text{NegativeBinomial}(s(x, v), \theta)$$

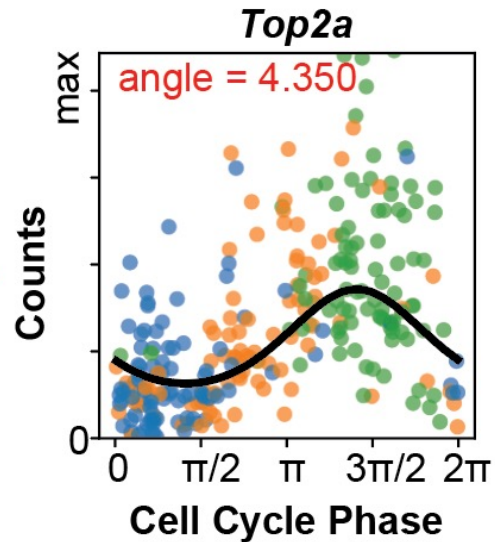
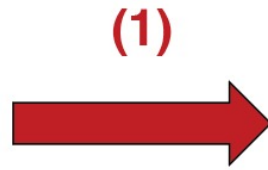
$$U \sim \text{NegativeBinomial}(u(x, v, \beta, \gamma, V(\cdot)), \theta)$$

# VeloCycle is a multivariate periodic velocity model

(1) Fit cell cycle phase and gene harmonics



scRNA-seq dataset

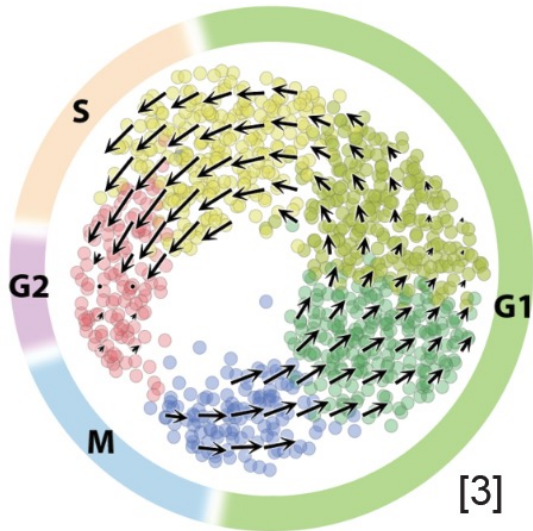


*“manifold learning”*

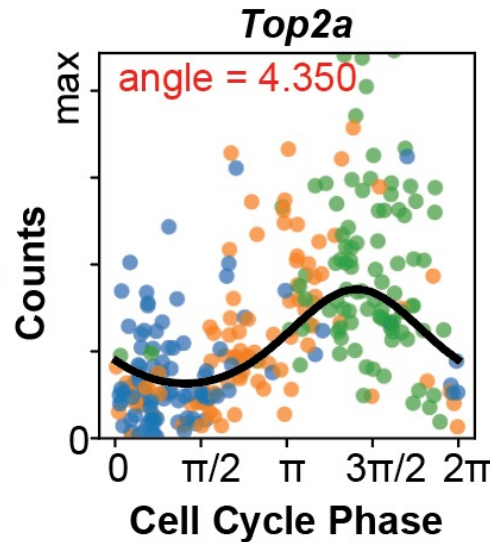
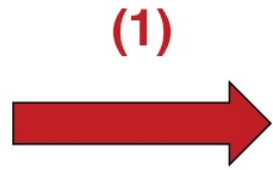
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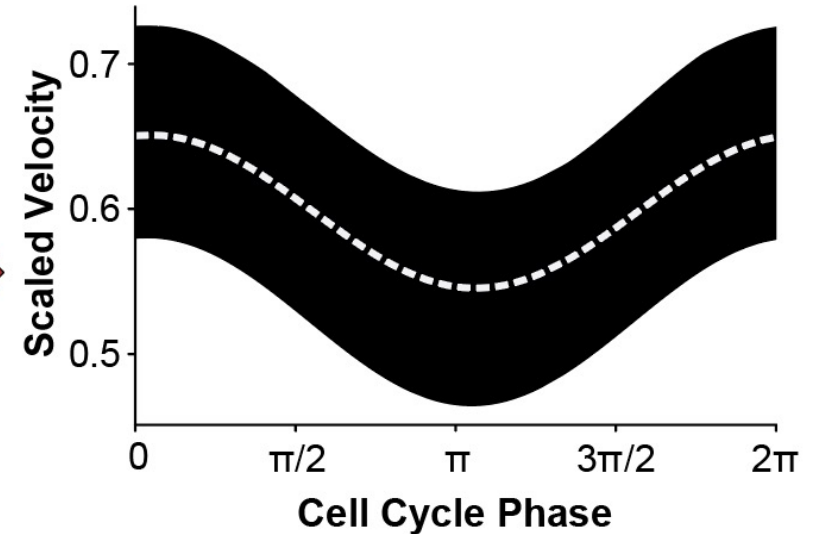
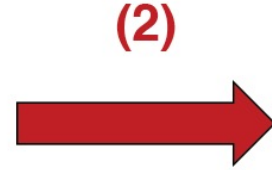
(2) Fit cell cycle velocity and kinetic parameters



scRNA-seq dataset



FACS label  
■ G1  
■ S  
■ G2M



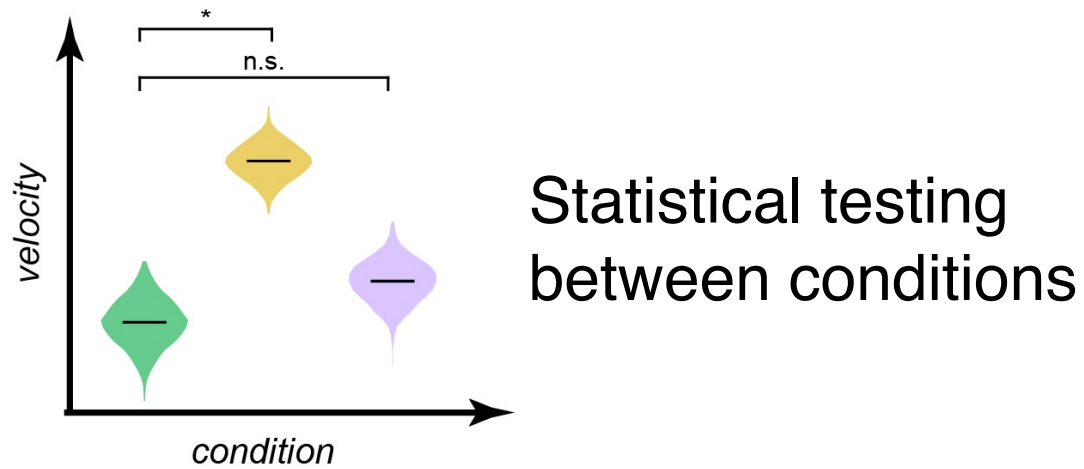
Convert velocity to hours time scale  
Perform velocity statistical tests  
Transfer learning of gene manifold

*“manifold learning”*

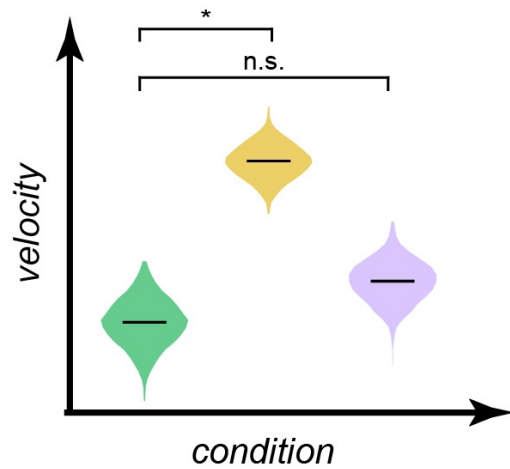
*“velocity learning”*



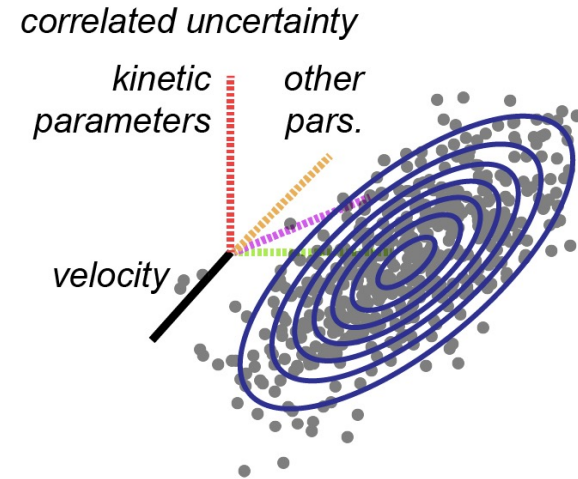
# VeloCycle is a versatile framework for manifold-constrained cell cycle velocity estimation



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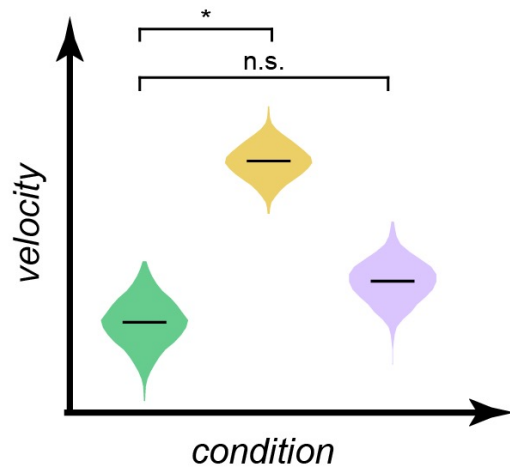


Statistical testing  
between conditions

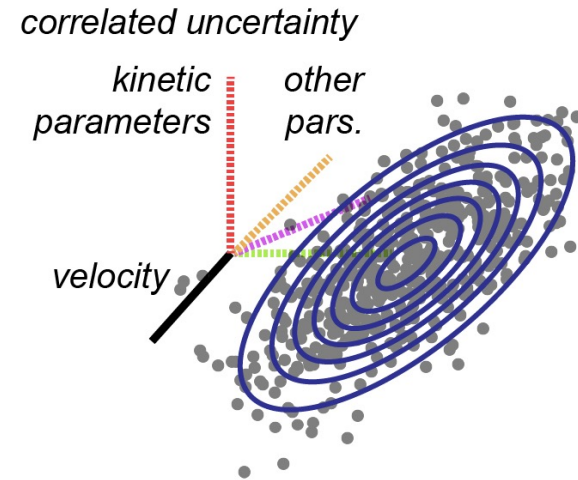


Structured posterior  
between velocity and  
kinetic parameters

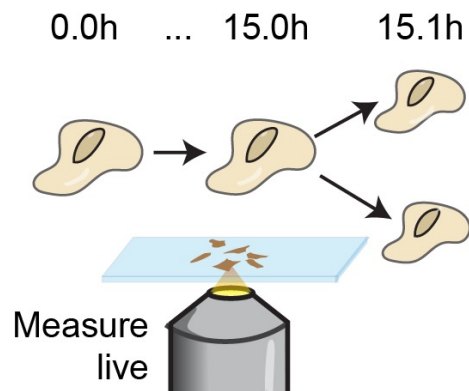
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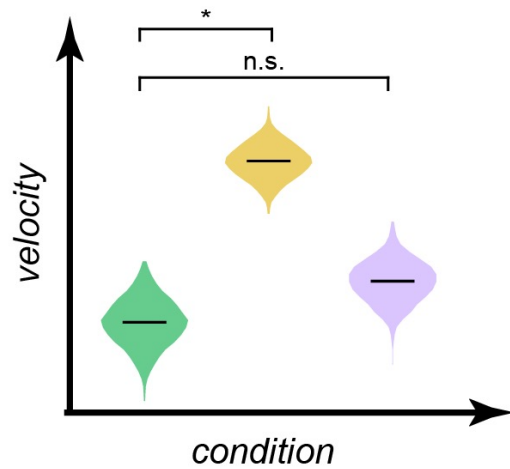


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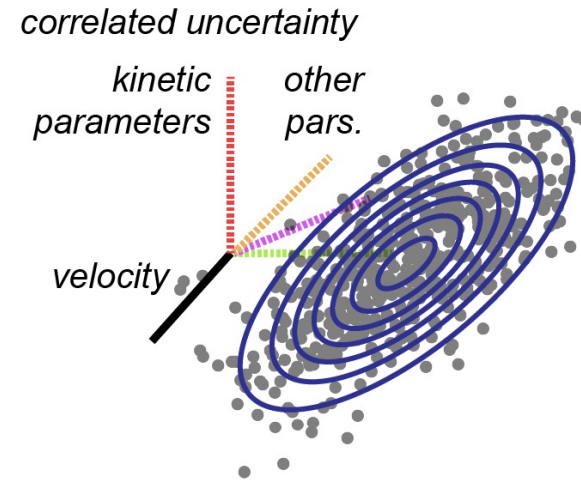


Experimental  
validation

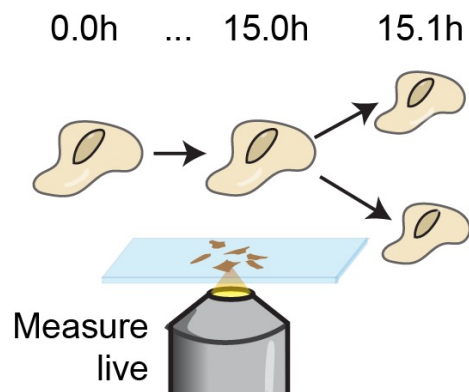
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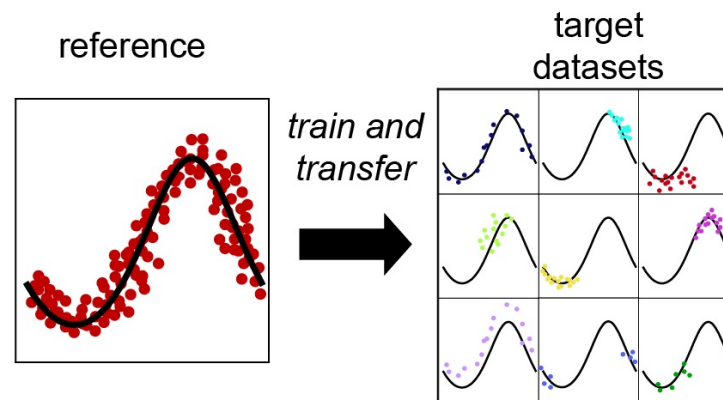
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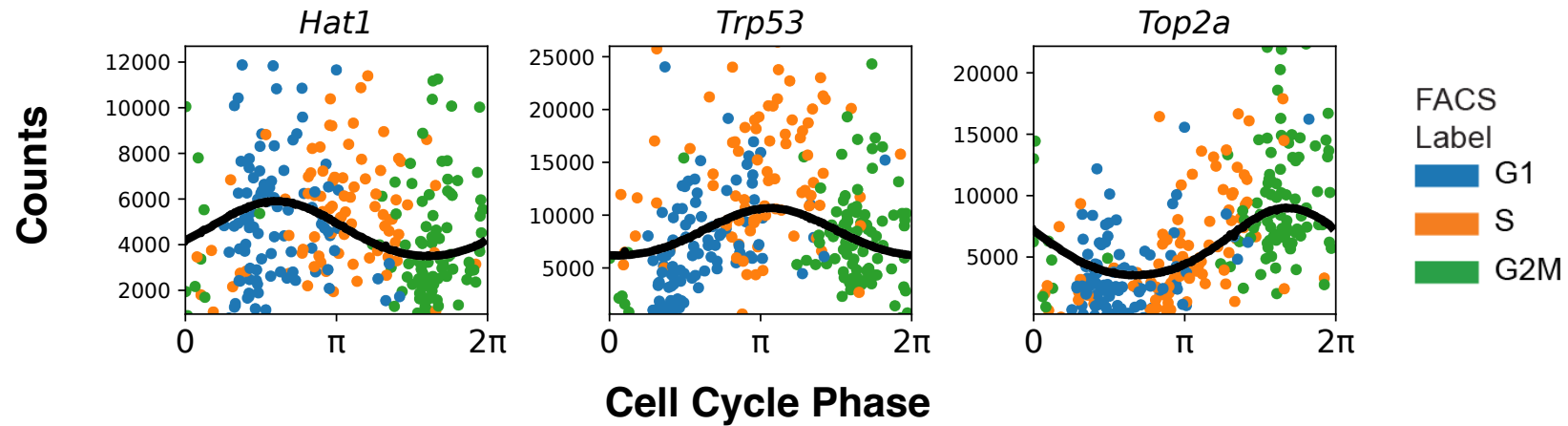
Experimental validation



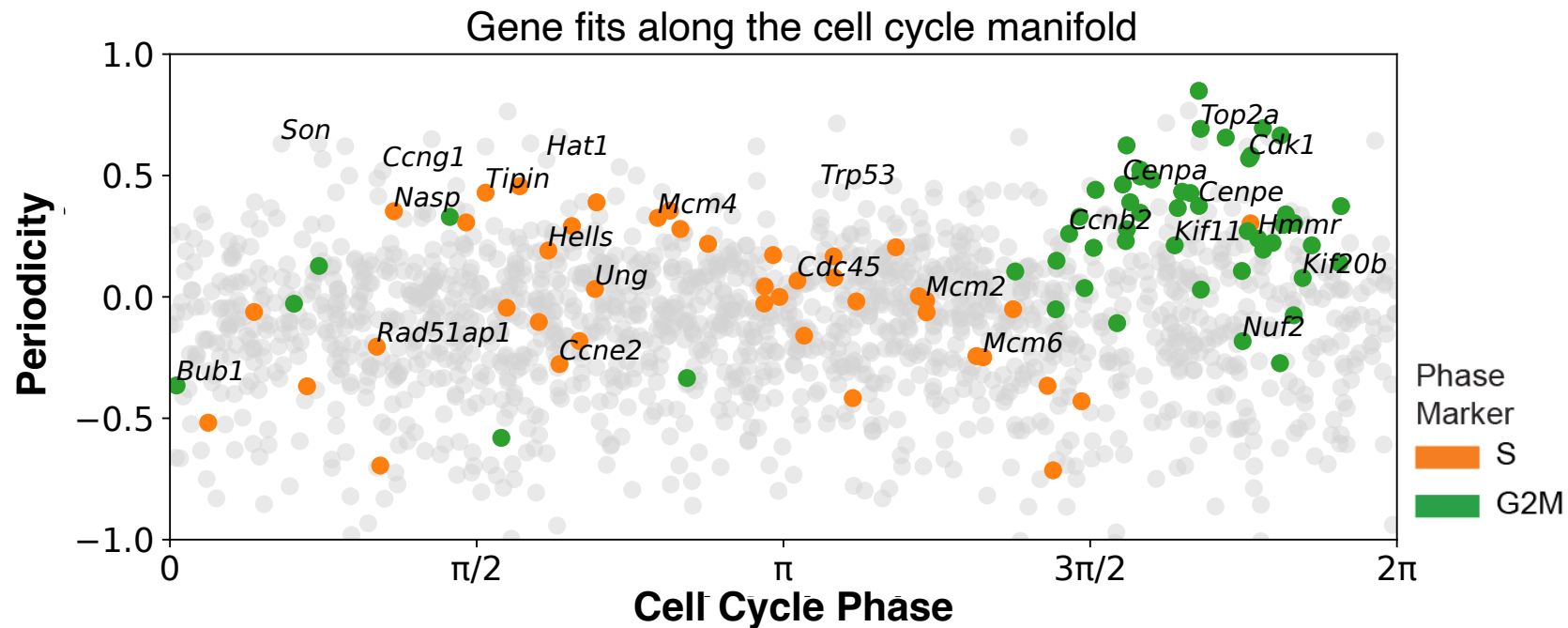
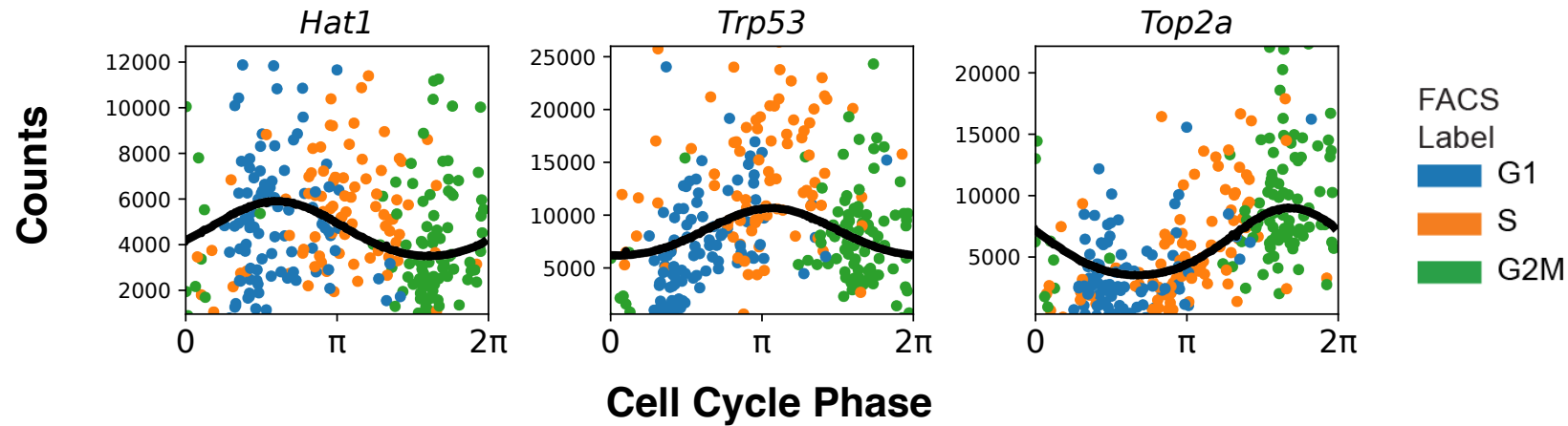
Transfer learning

**Does manifold-learning recover accurate cell cycle phases?**

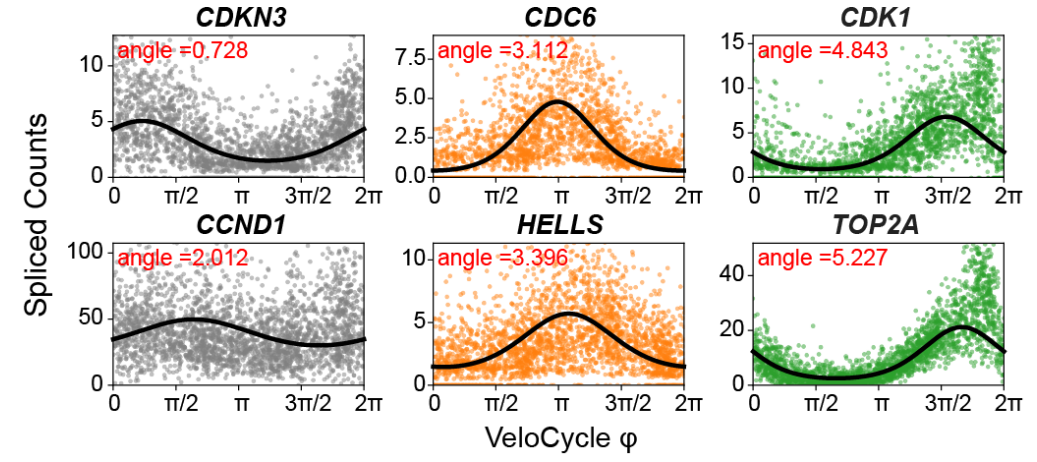
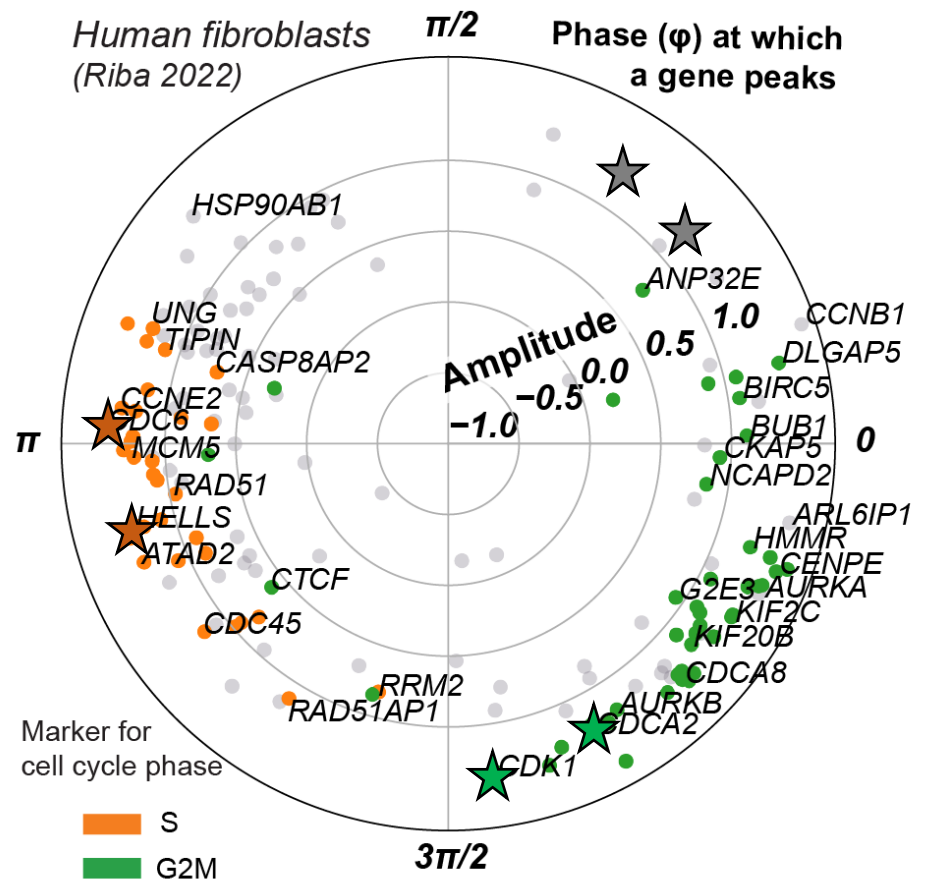
# Phase assignments can be validated with FACS-sorted mESCs



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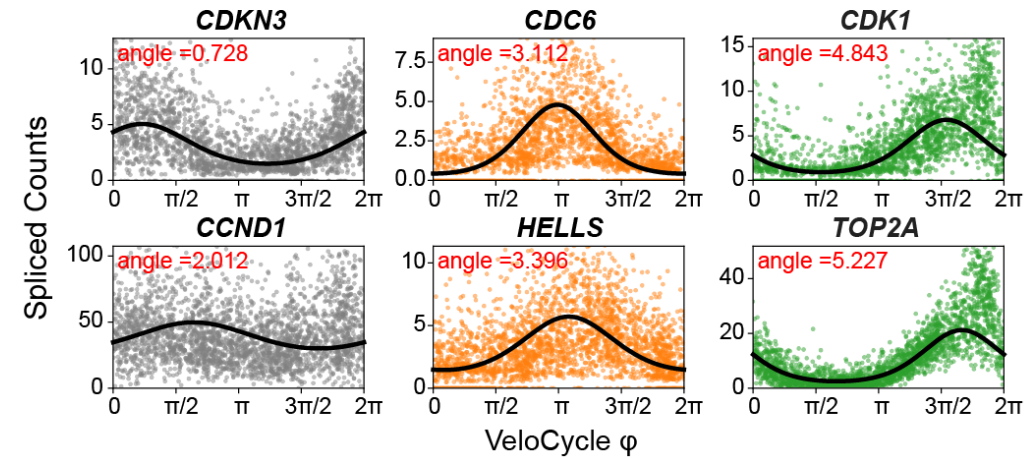
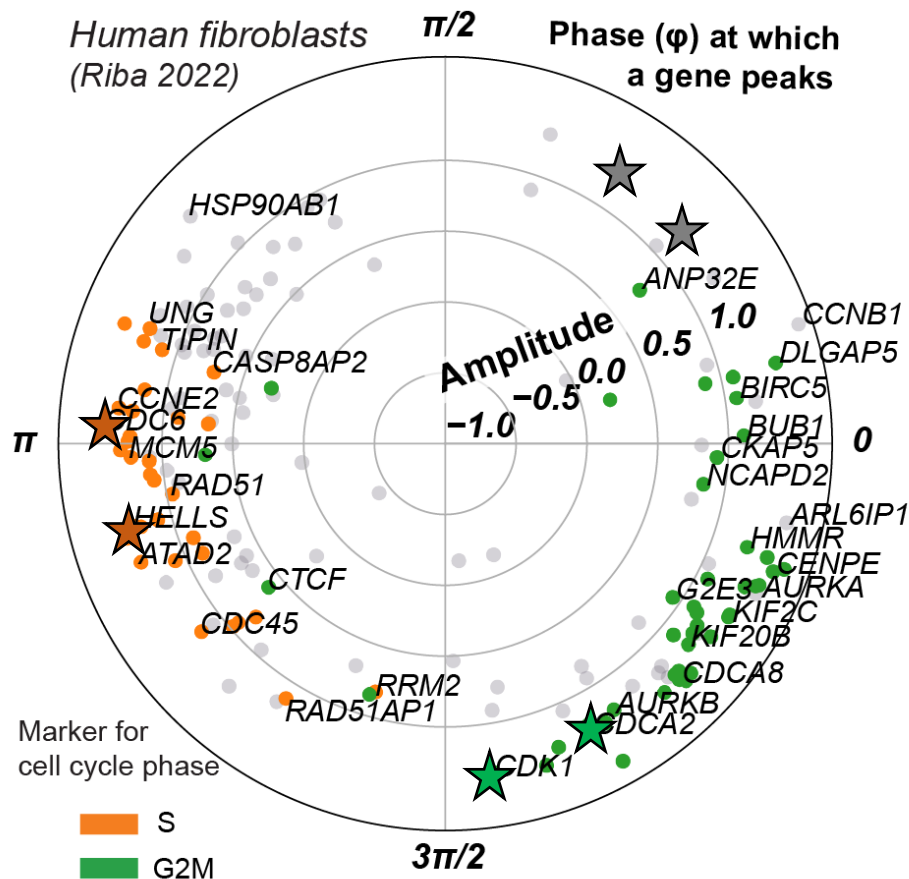


# VeloCycle manifold-learning estimates accurate and robust phases

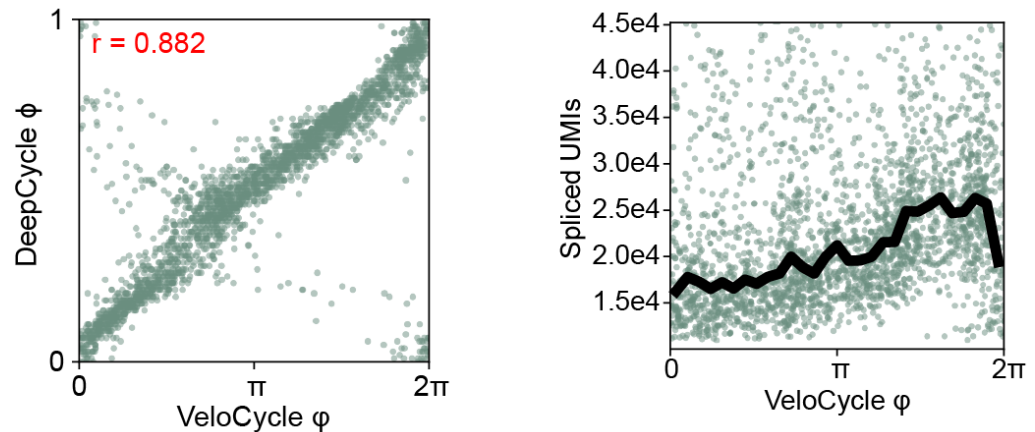




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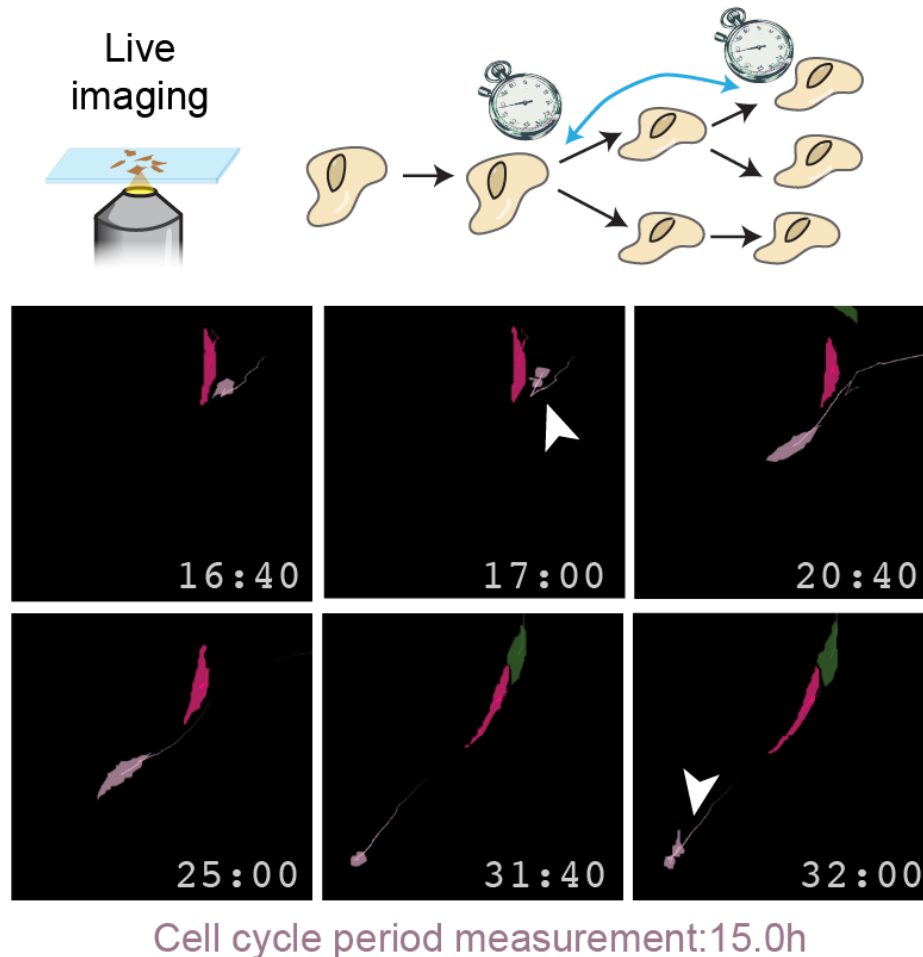


Phase comparison



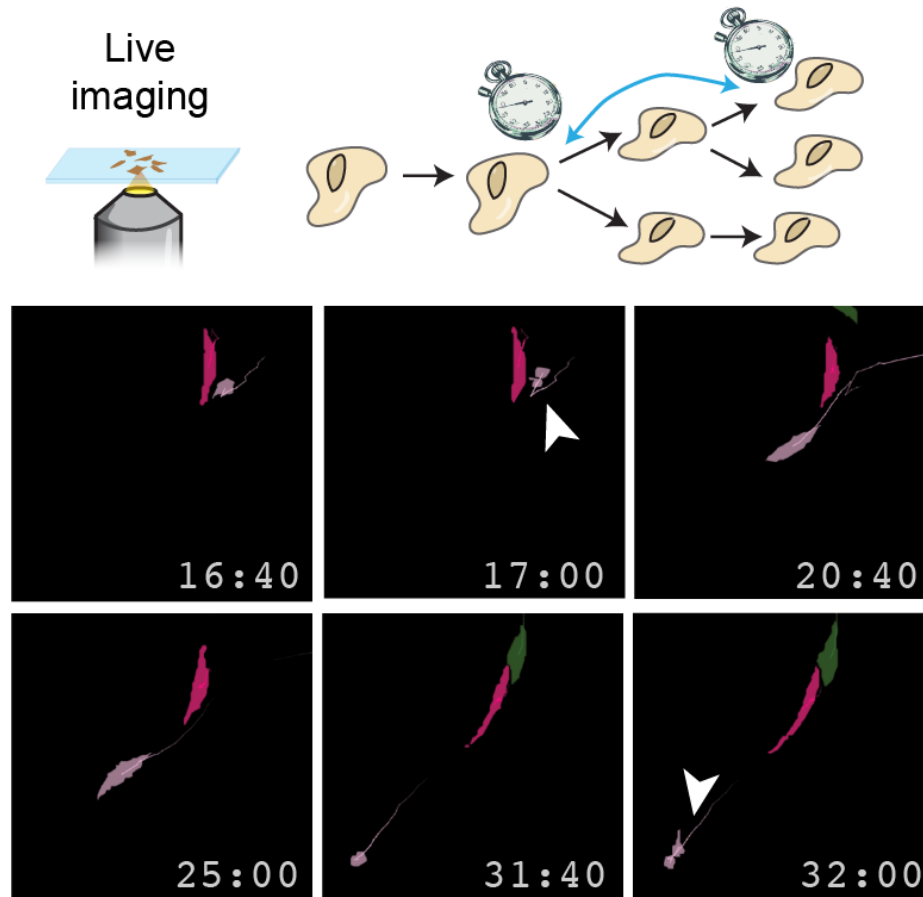
**Can we experimentally validate our cell cycle speed estimates?**

# Time-lapse microscopy validates computationally inferred cell cycle speeds

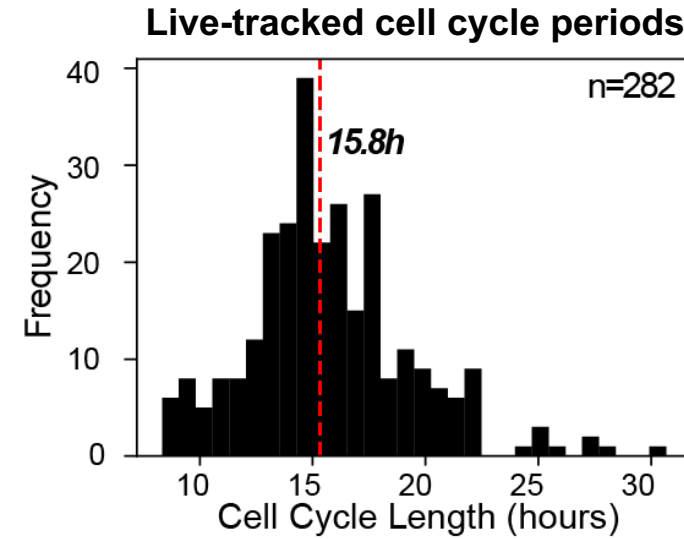


Dataset from: Capolupo et al. 2022

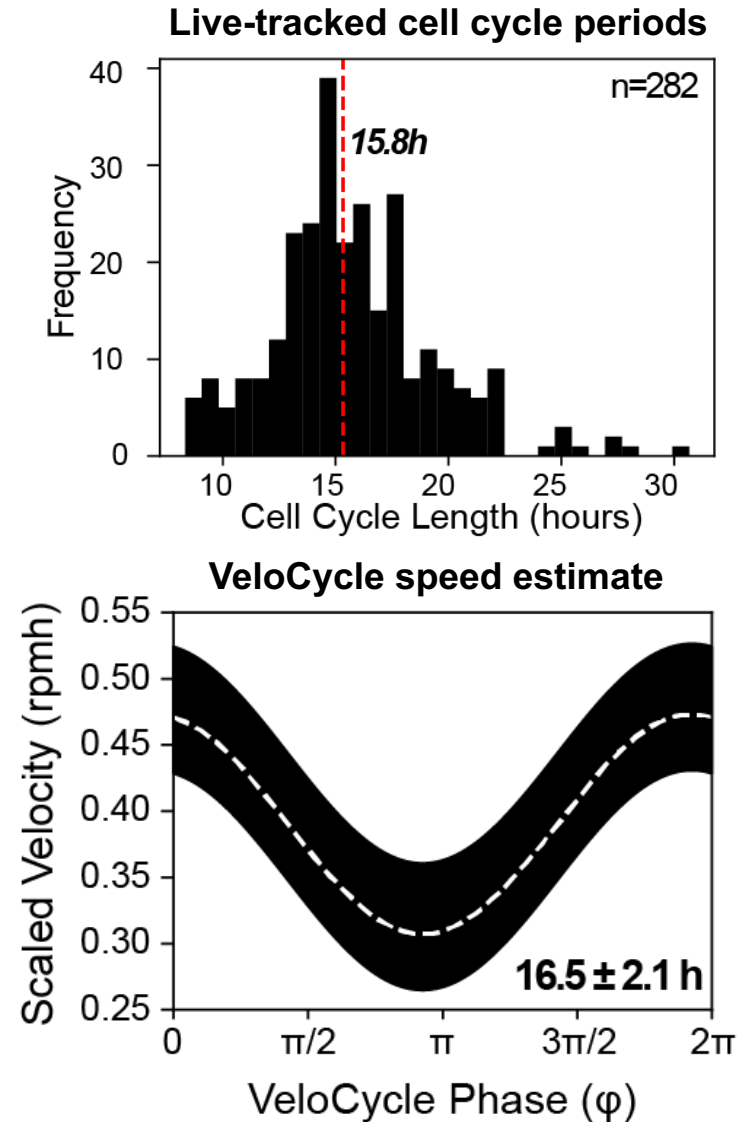
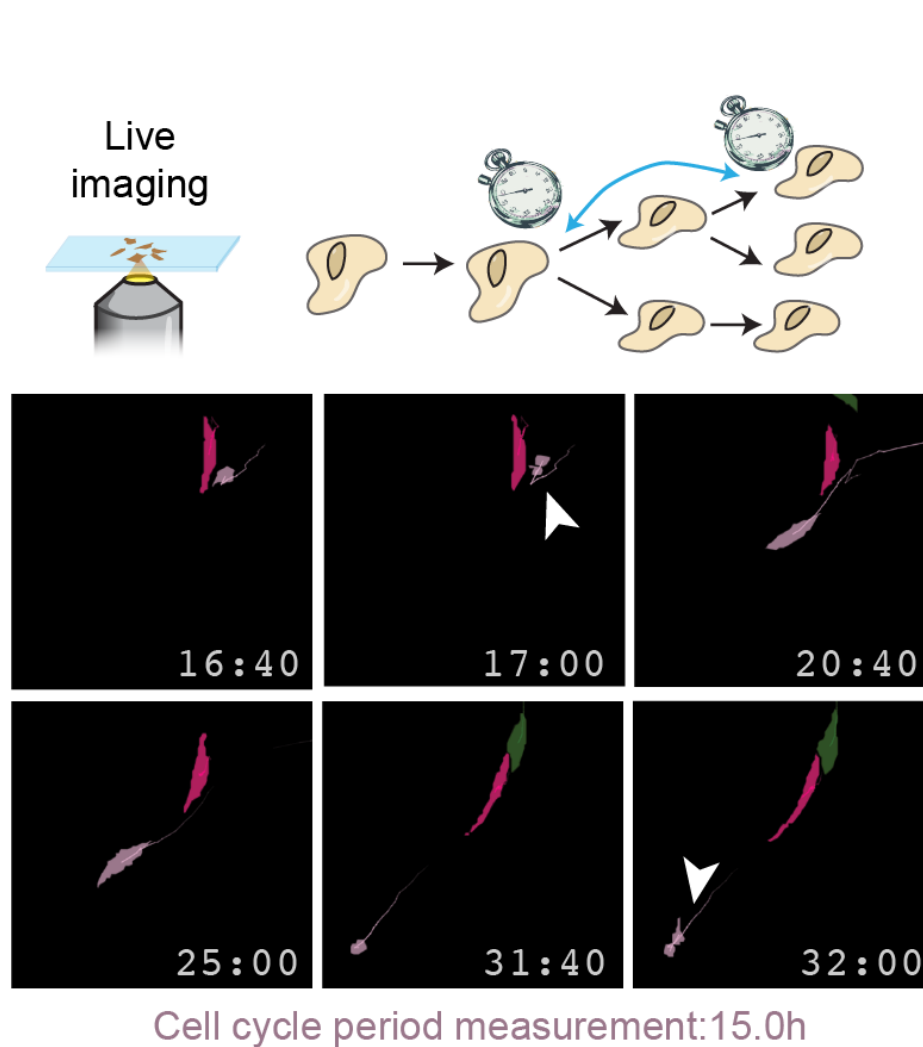
# Time-lapse microscopy validates computationally inferred cell cycle speeds



Cell cycle period measurement: 15.0h

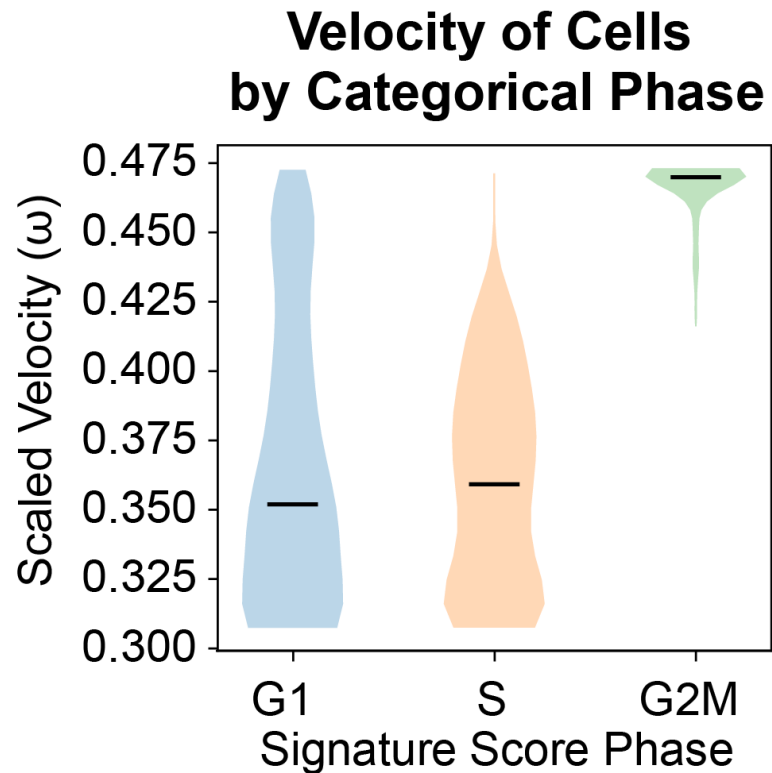


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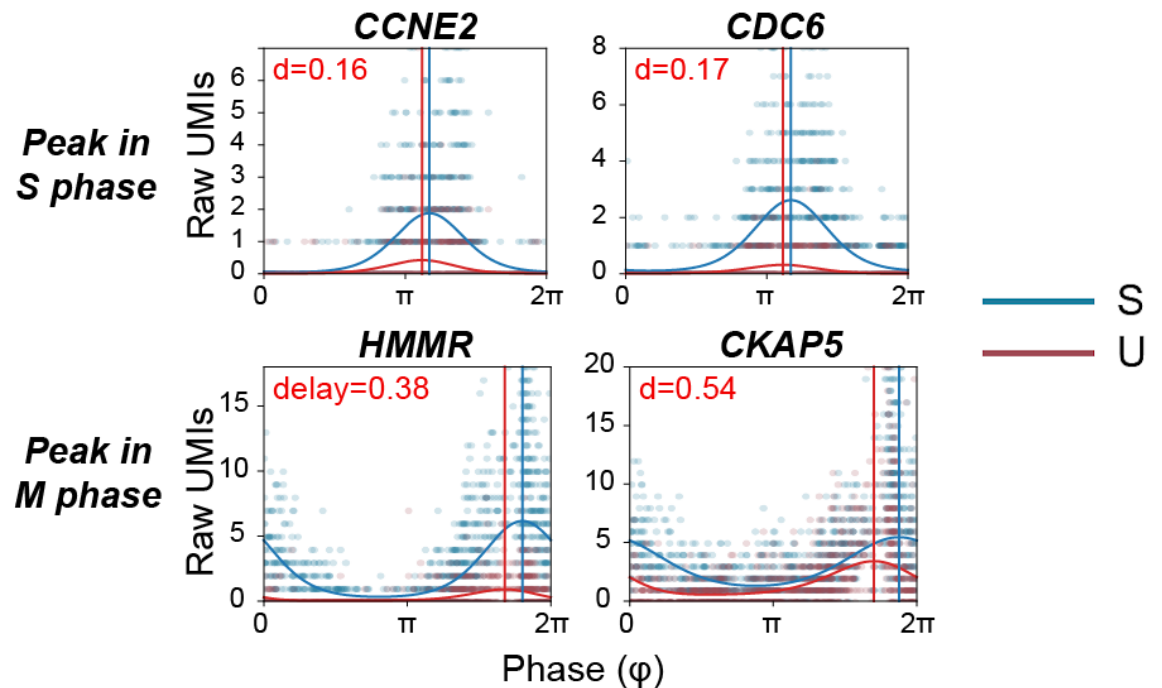
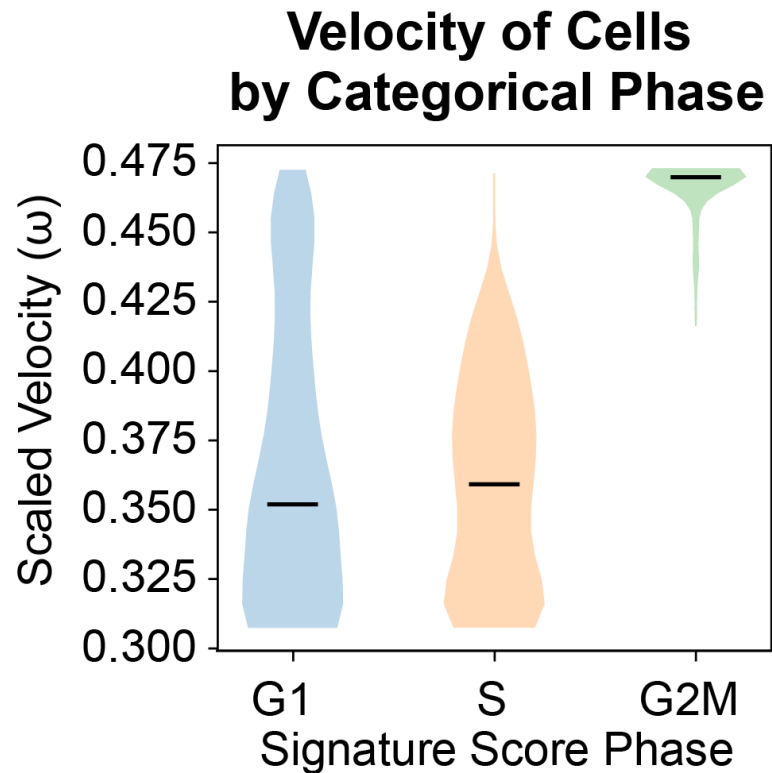


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# Velocity estimates vary by phase and correspond to the unspliced-spliced expression delay



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**Does the rate of the cell cycle vary across different tissues and environmental contexts?**



# Credibility testing of cell cycle velocity before and after cell treatment with erlotinib

PC9 cancer cell line

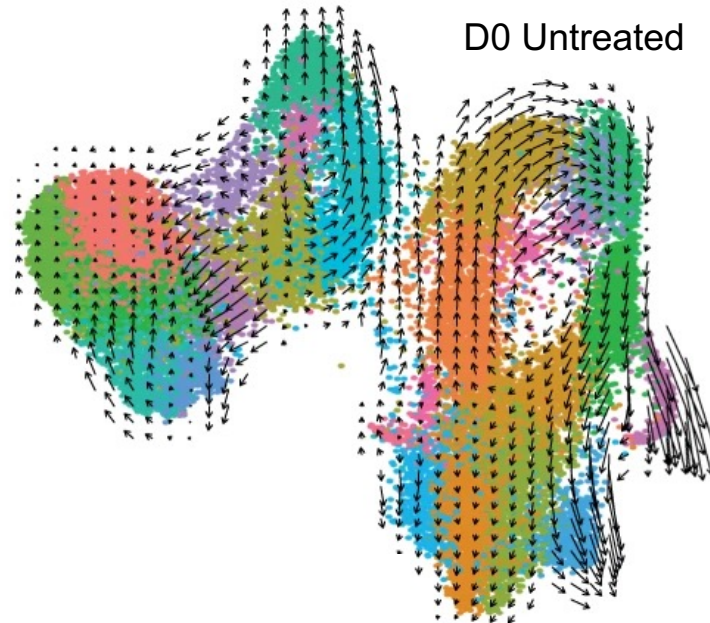
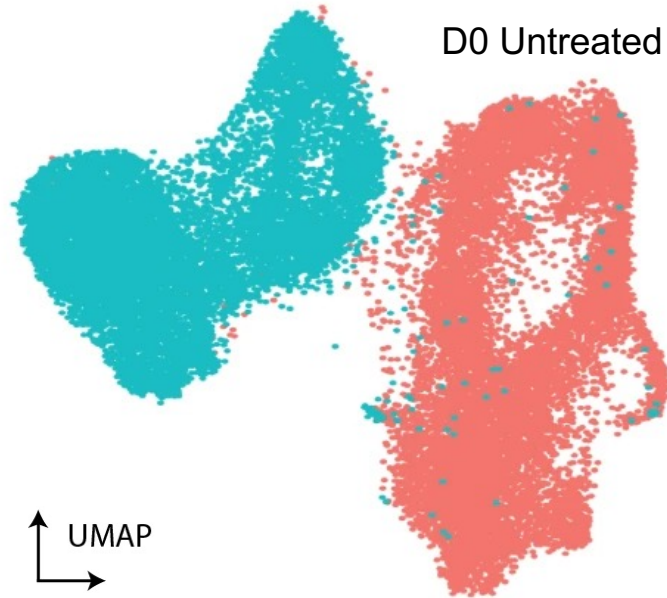
Steady-state velocity analysis

D3 Treated (Erlotinib)

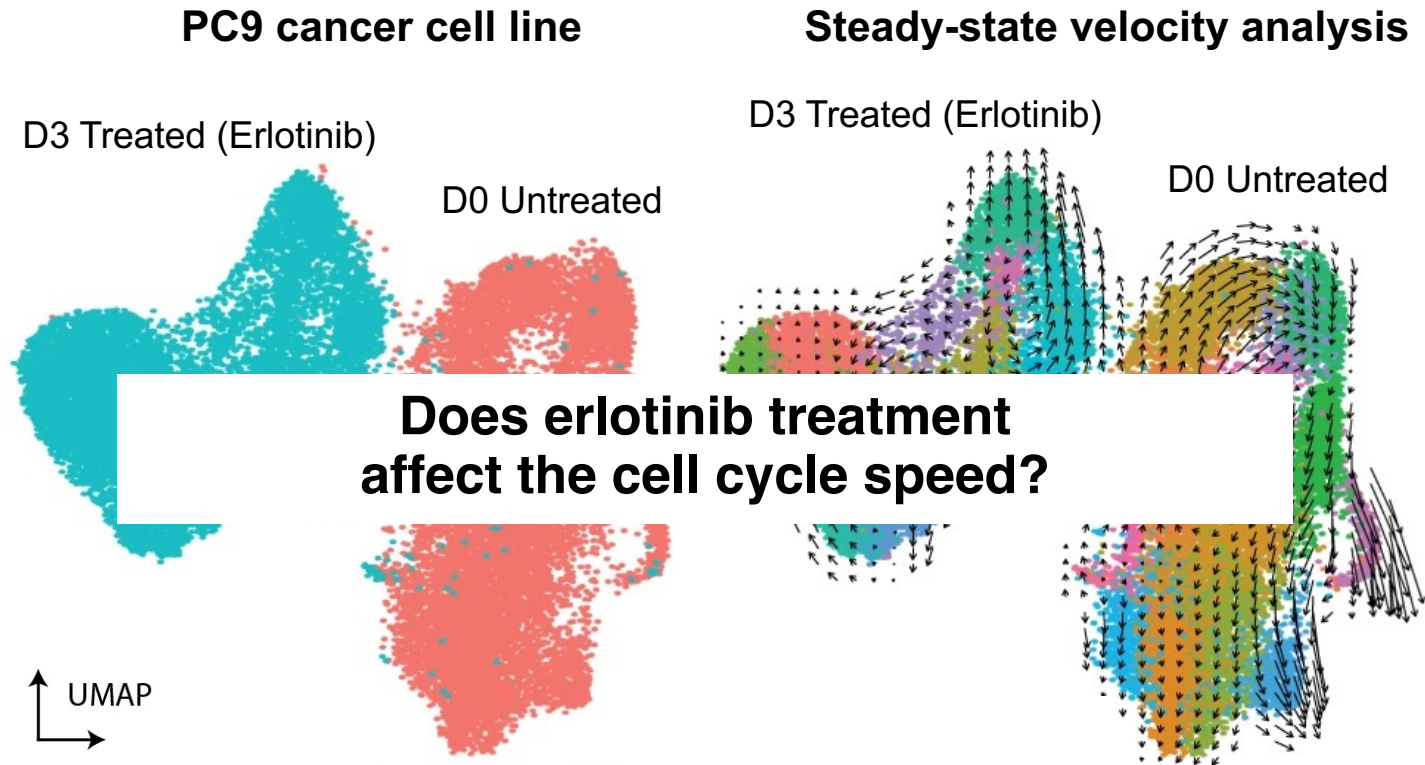
D3 Treated (Erlotinib)

D0 Untreated

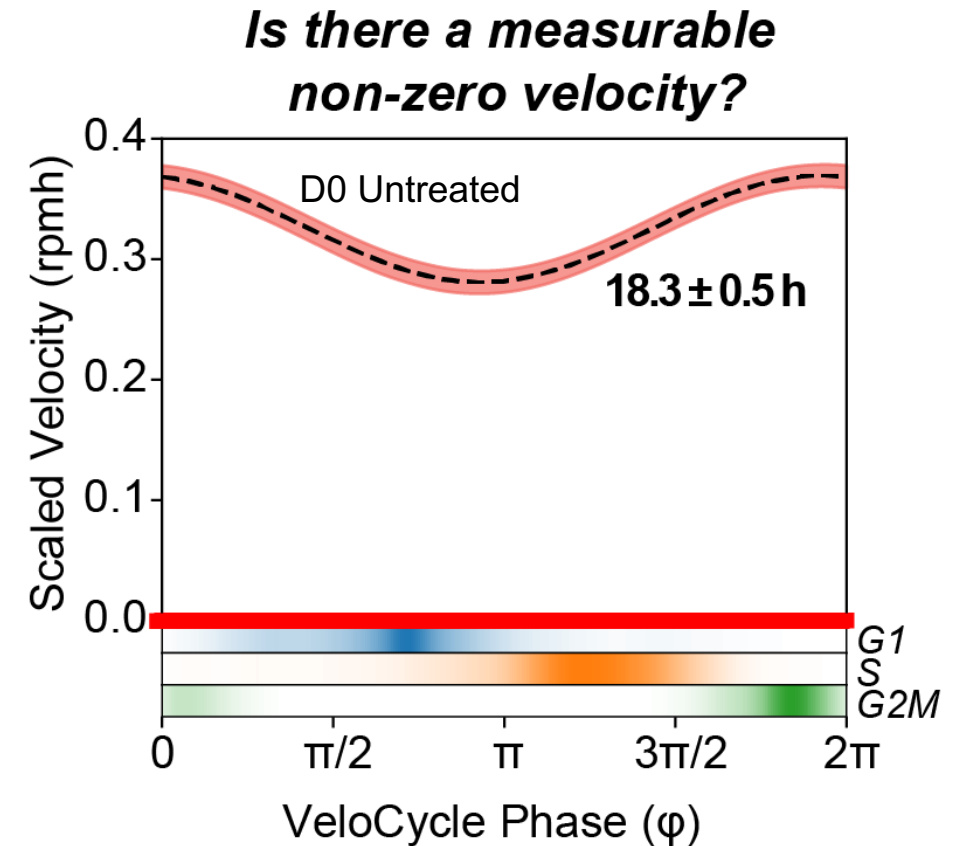
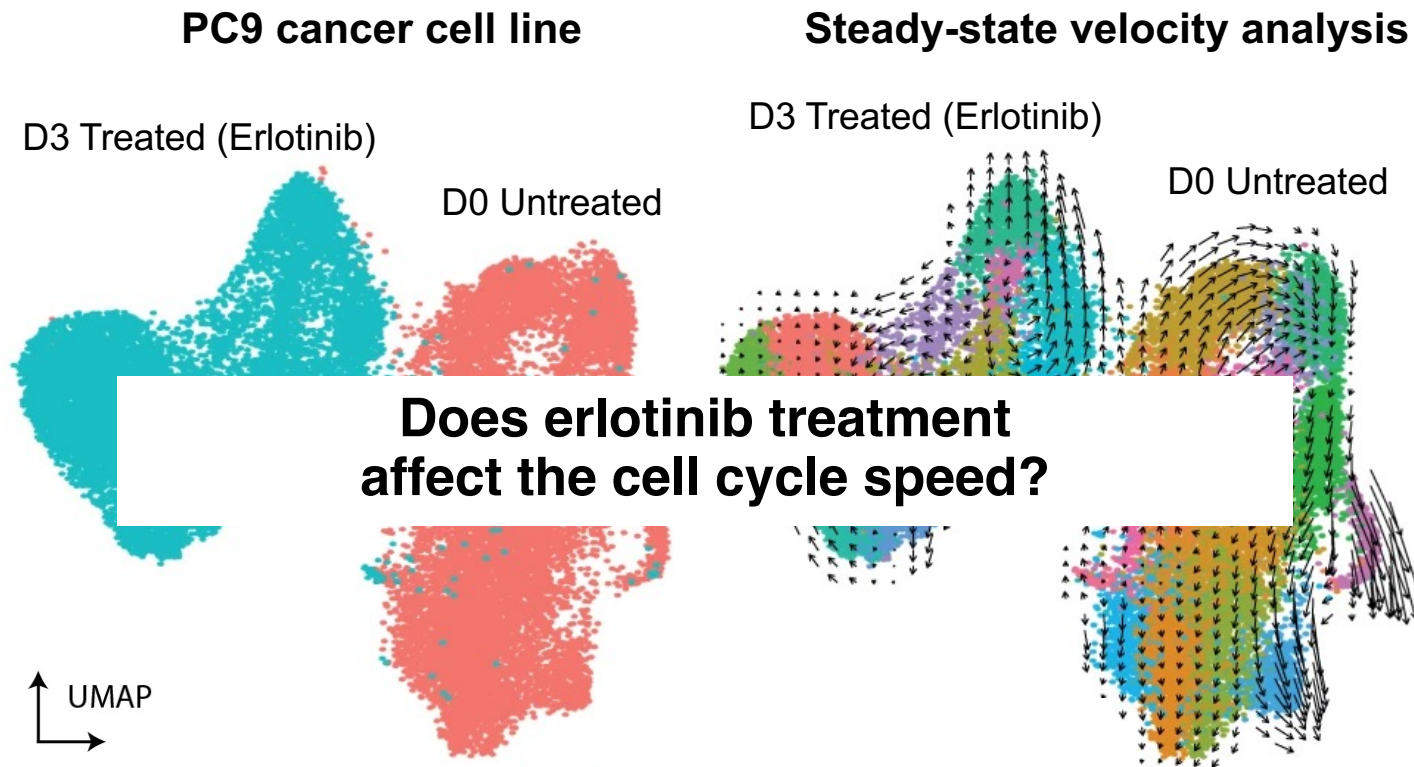
D0 Untreated



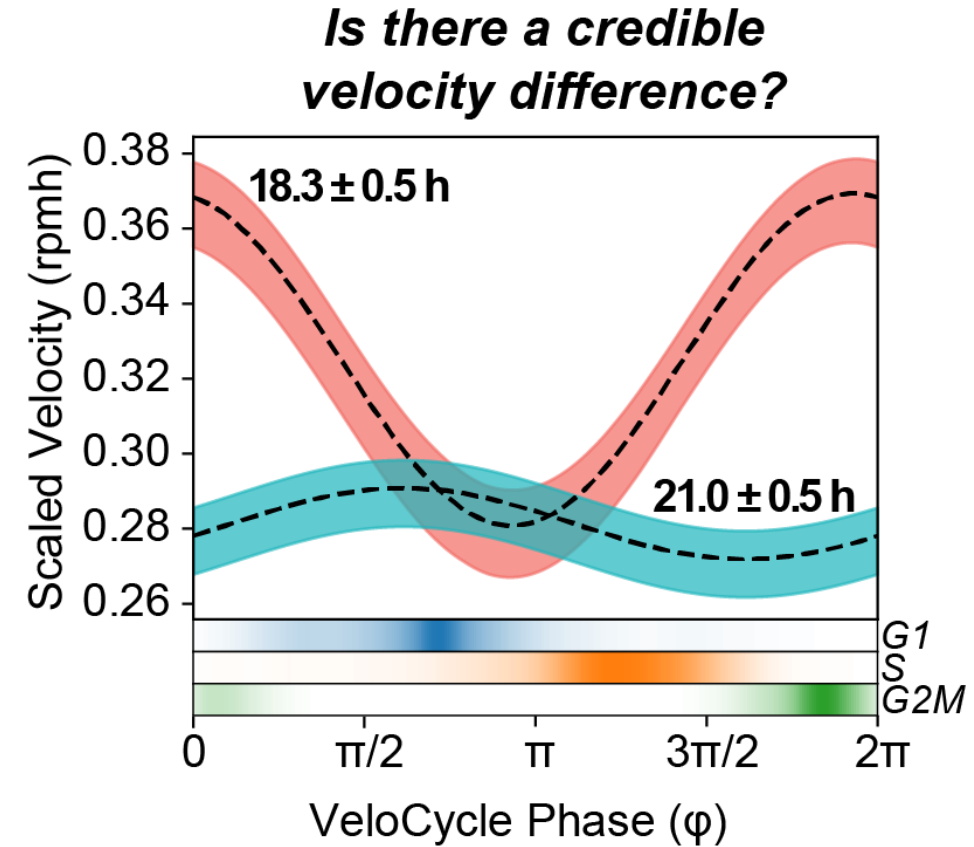
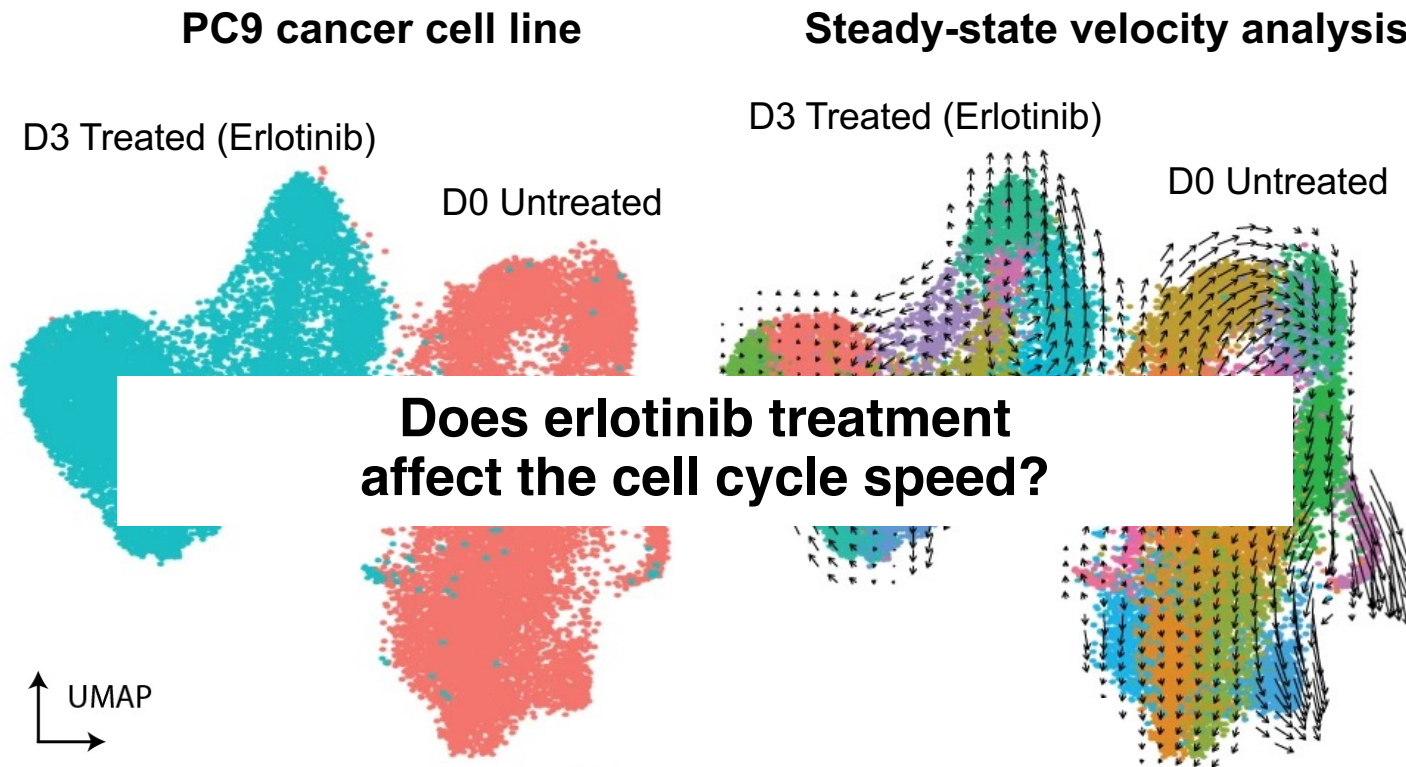
# Credibility testing of cell cycle velocity before and after cell treatment with erlotinib



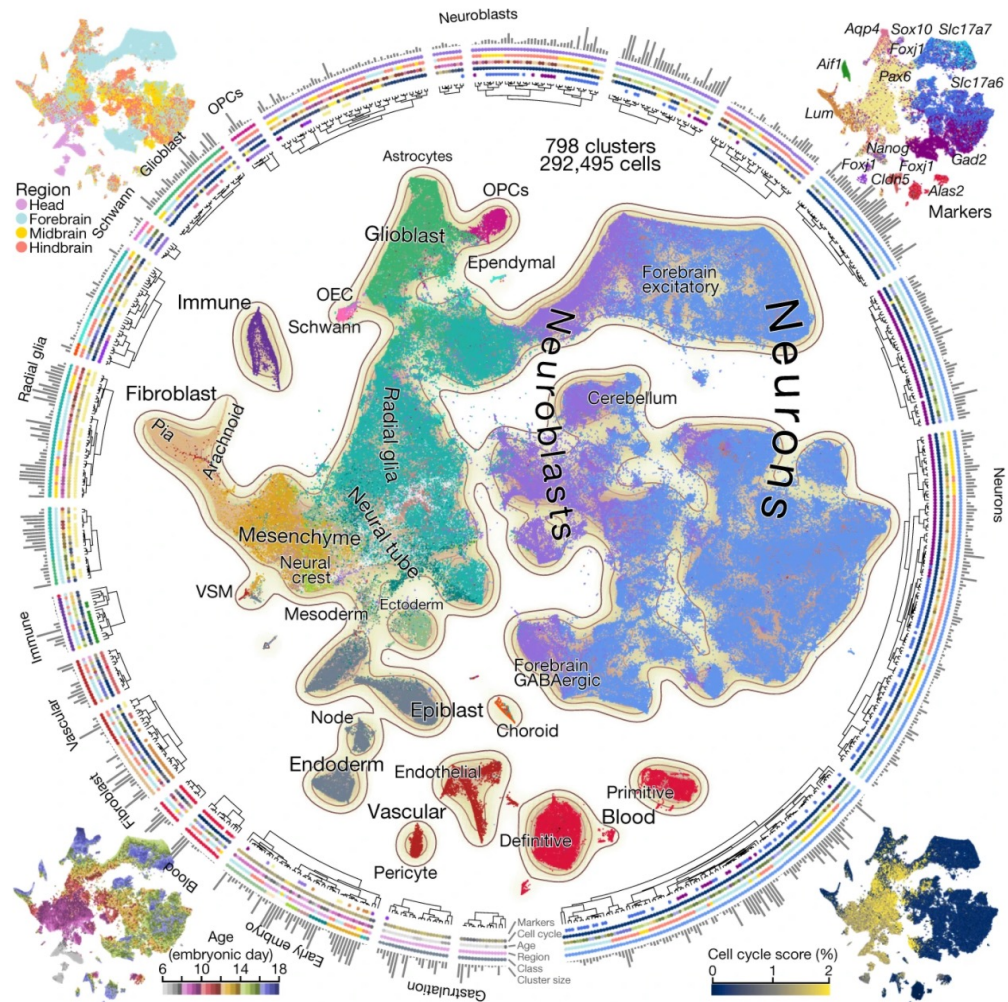
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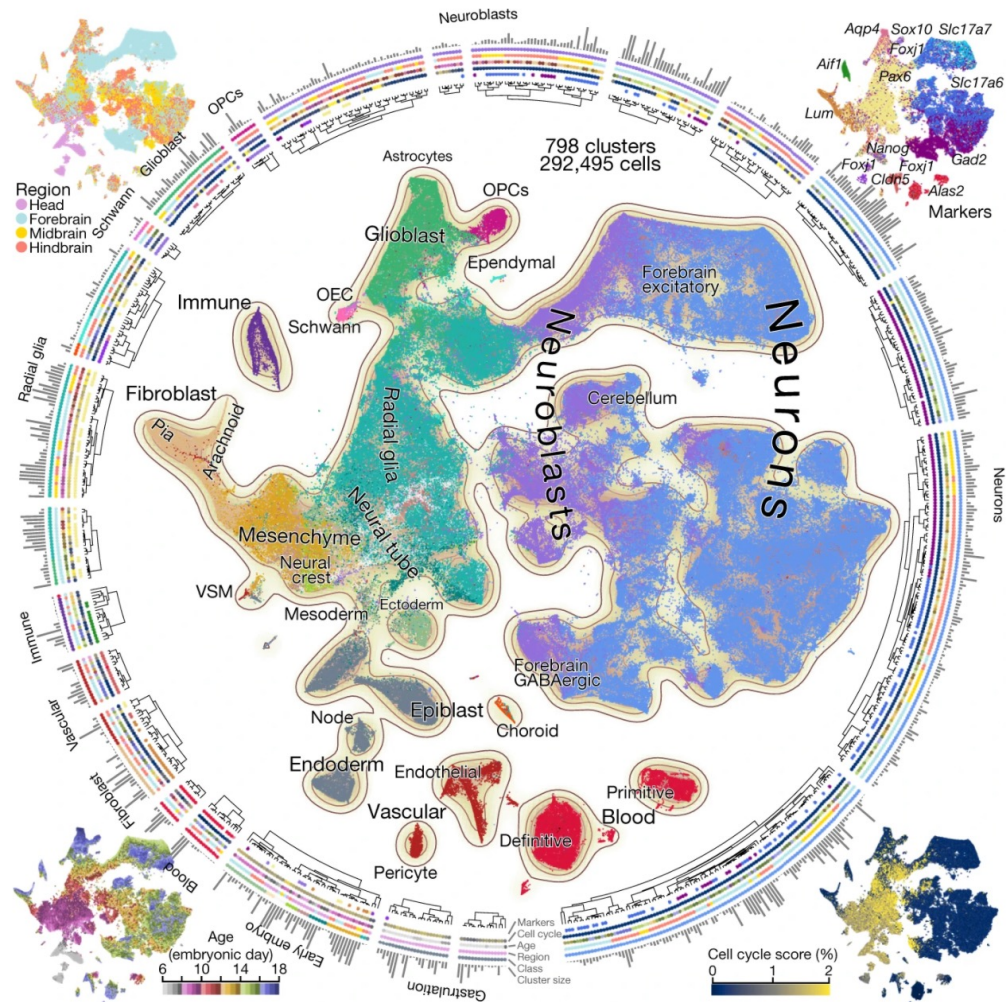
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# Cell cycle speed in radial glial progenitors varies along a spatio-temporal axis in mouse development

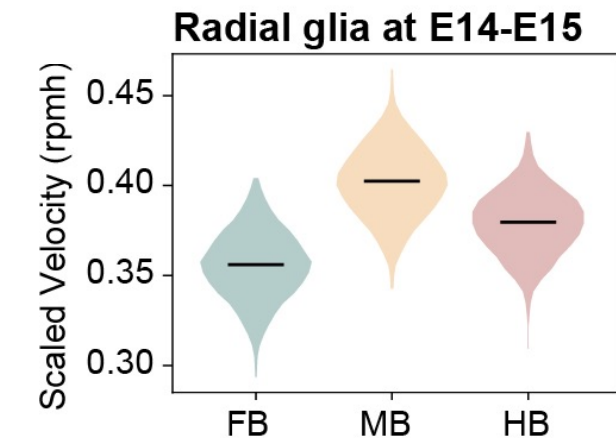
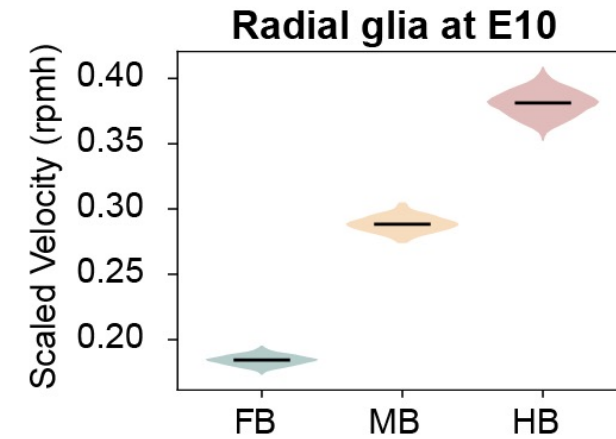
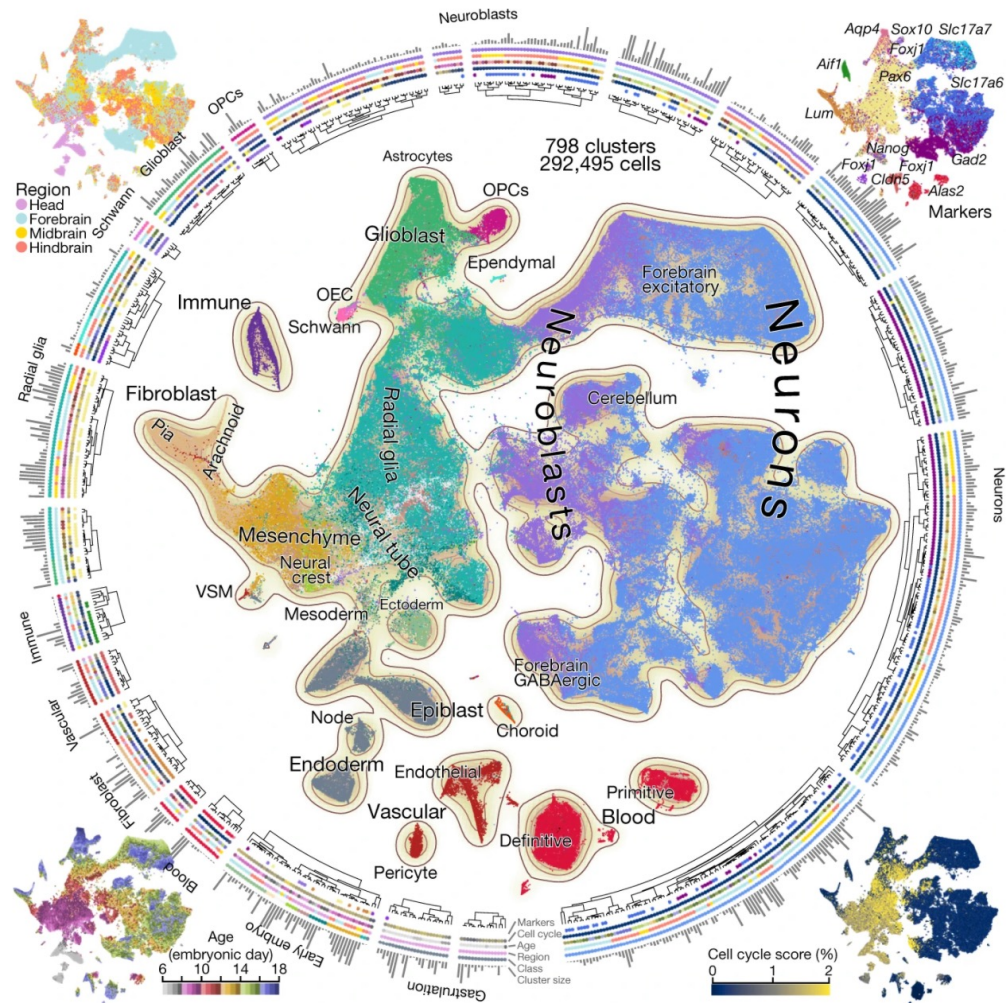


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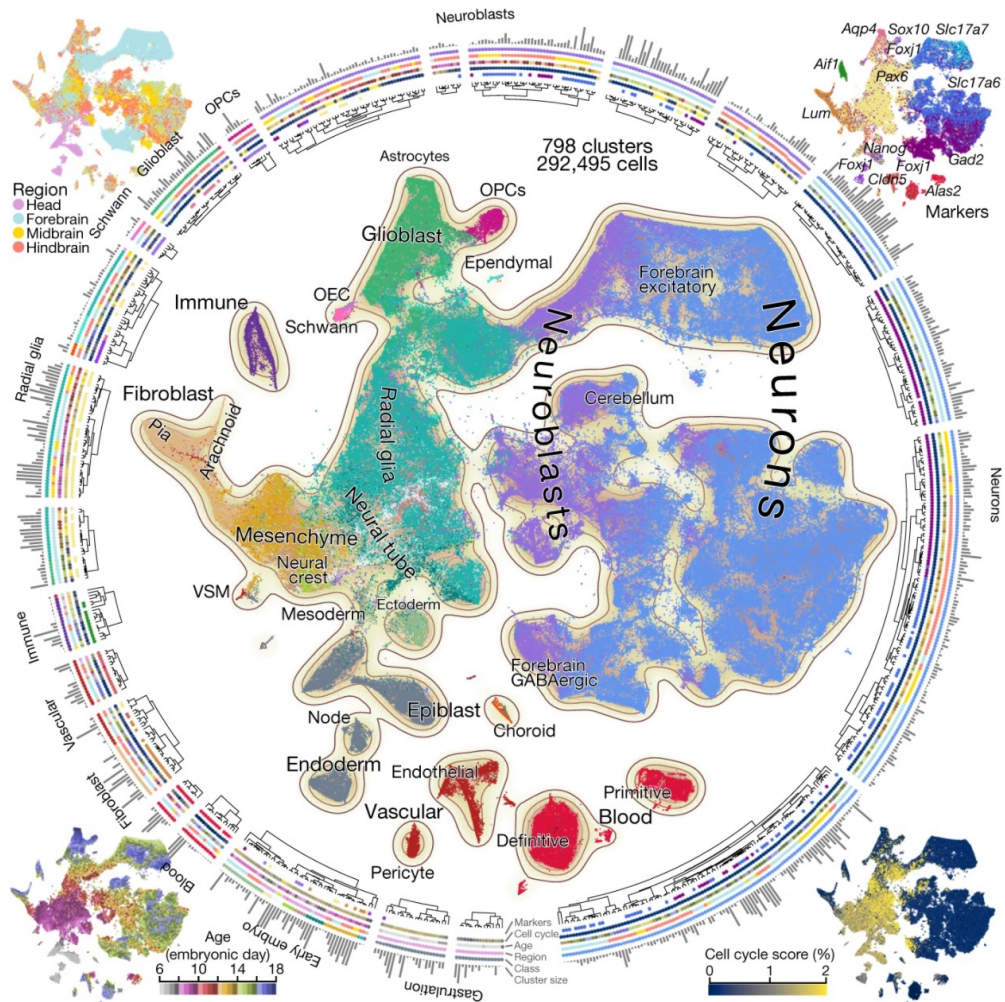


**Does the cell cycle speed vary in brain progenitors from different spatial regions?**

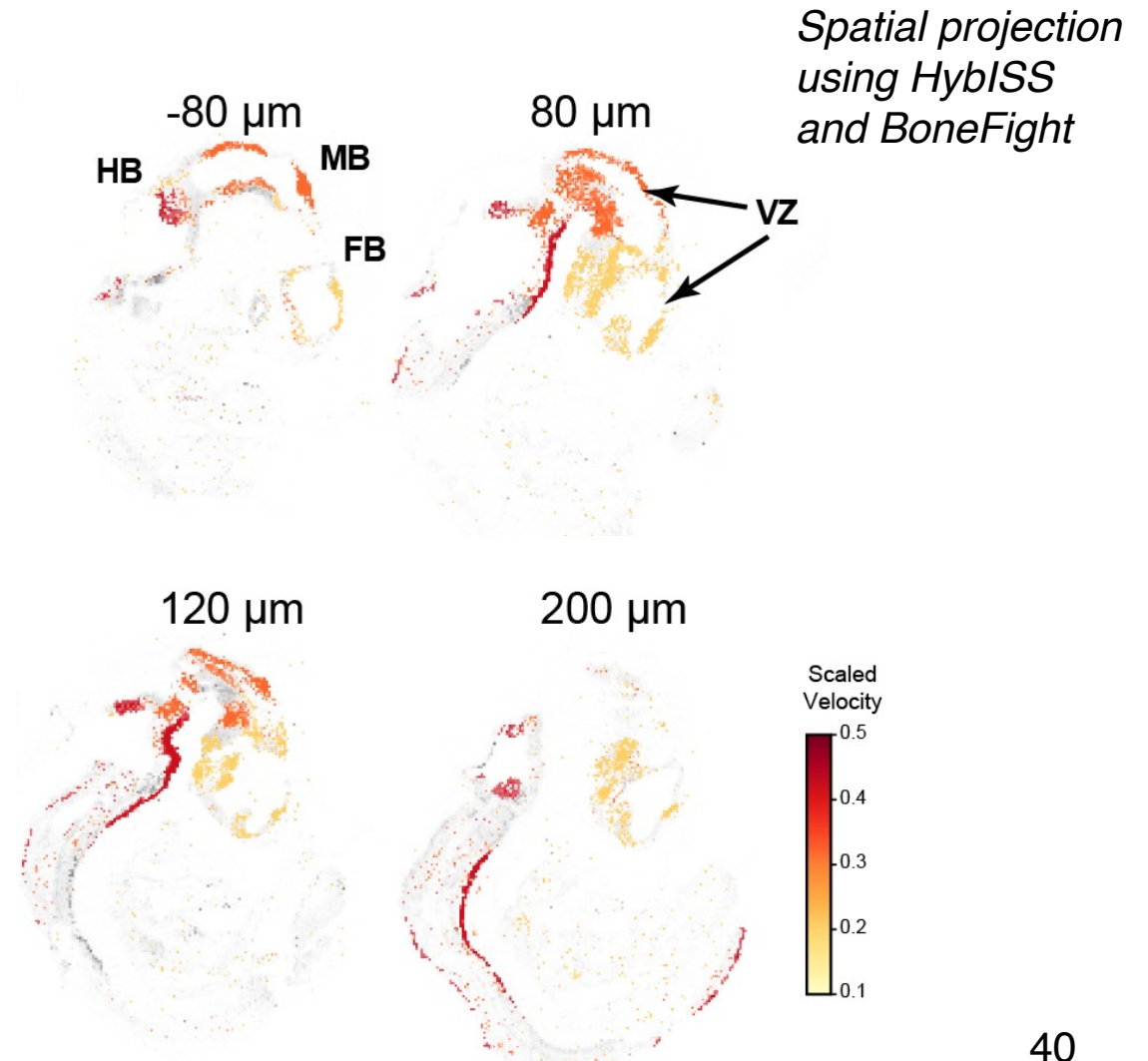
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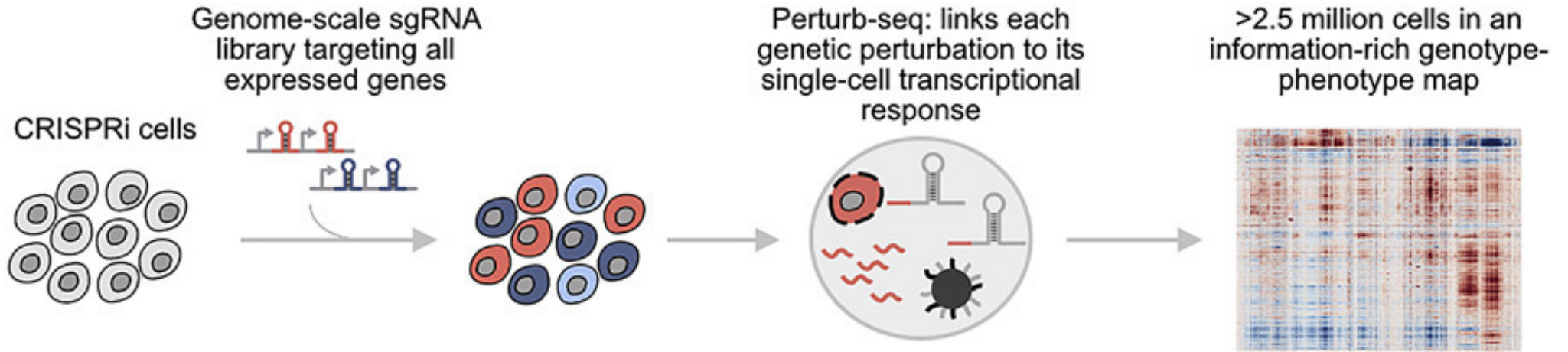


La Manno et al 2021



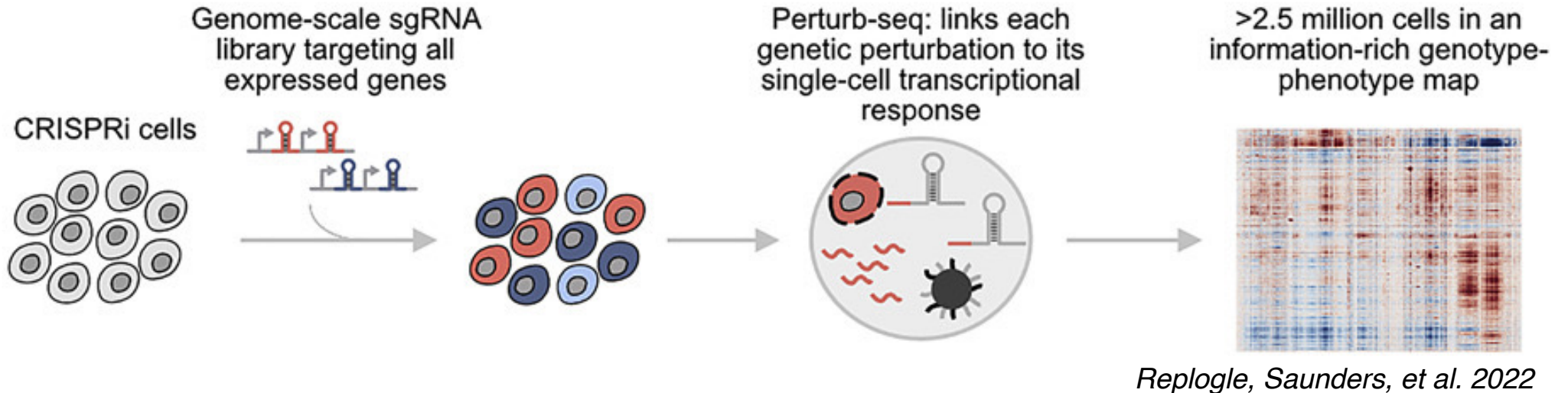


# Genome-wide Perturb-seq constructs a comprehensive genotype-phenotype map



*Replogle, Saunders, et al. 2022*

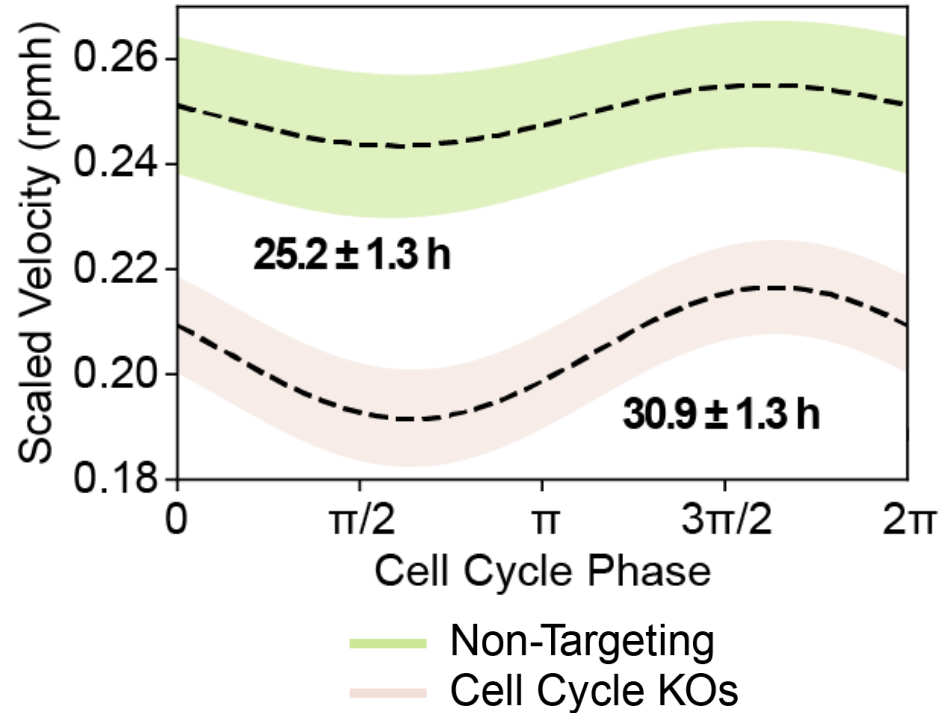
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How do single-gene knockdowns affect the cell cycle speed?

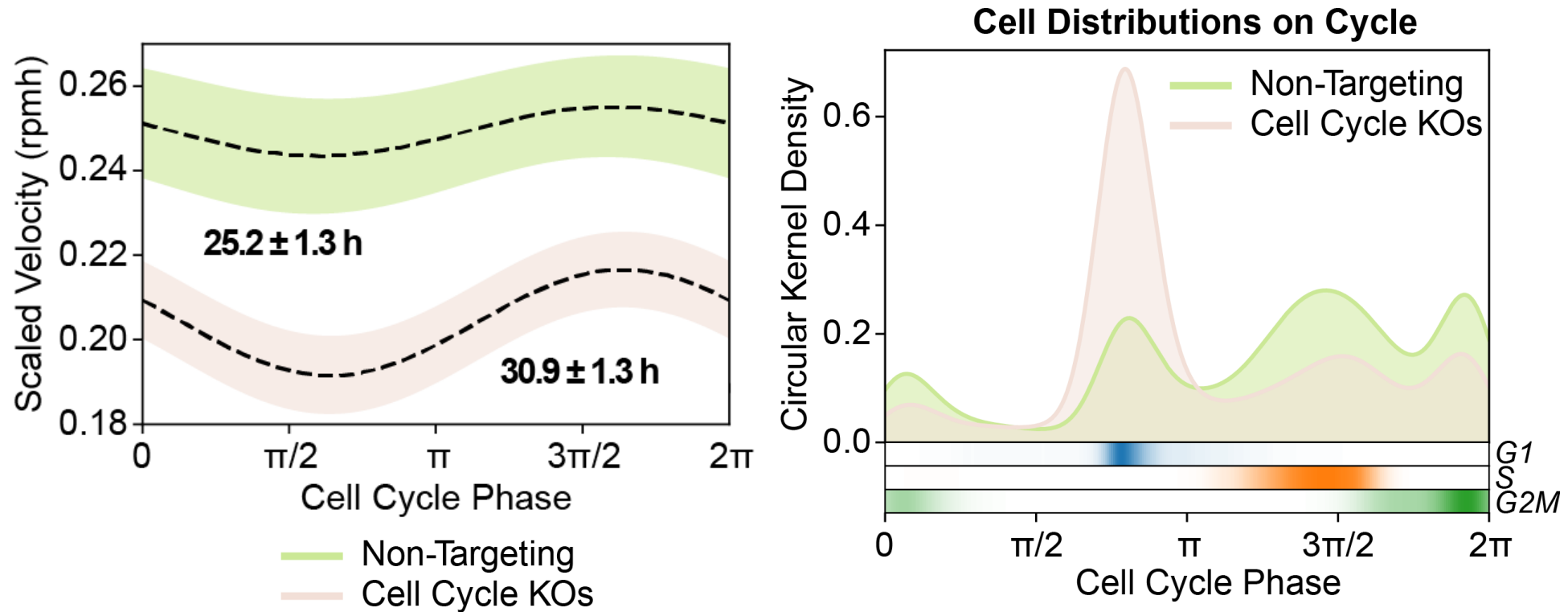
Challenge: there are **very few cells** for each perturbation condition.

# Cells containing a targeted knock-down of a cell cycle gene have a slower cell cycle velocity and more G1 cells



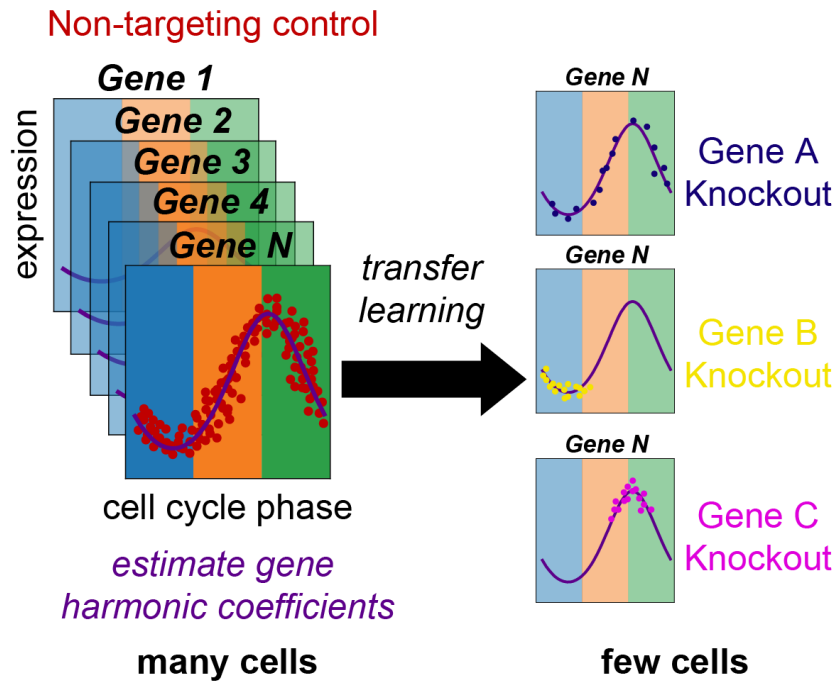
- Genome-wide Perturb-seq dataset in RPE1 cell line

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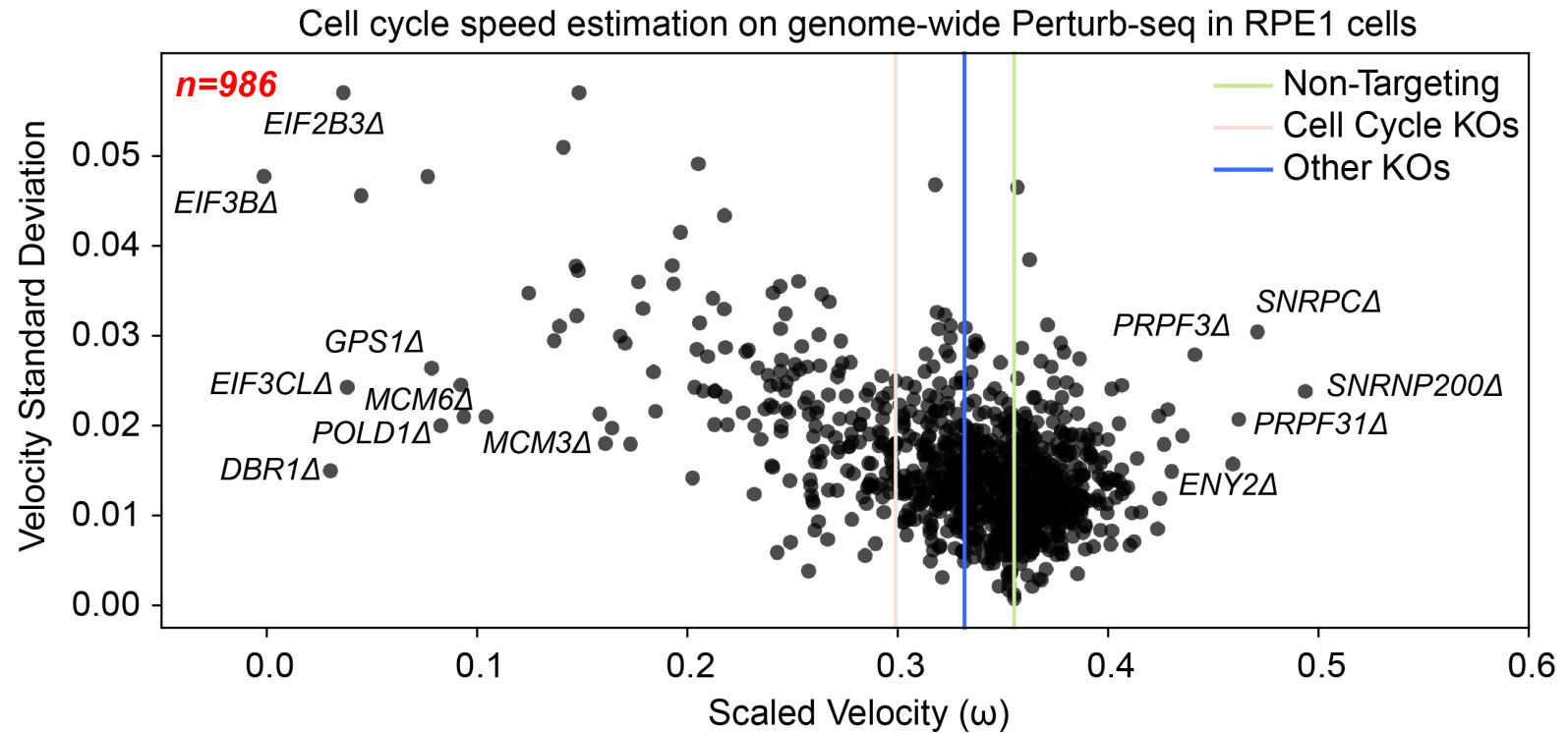
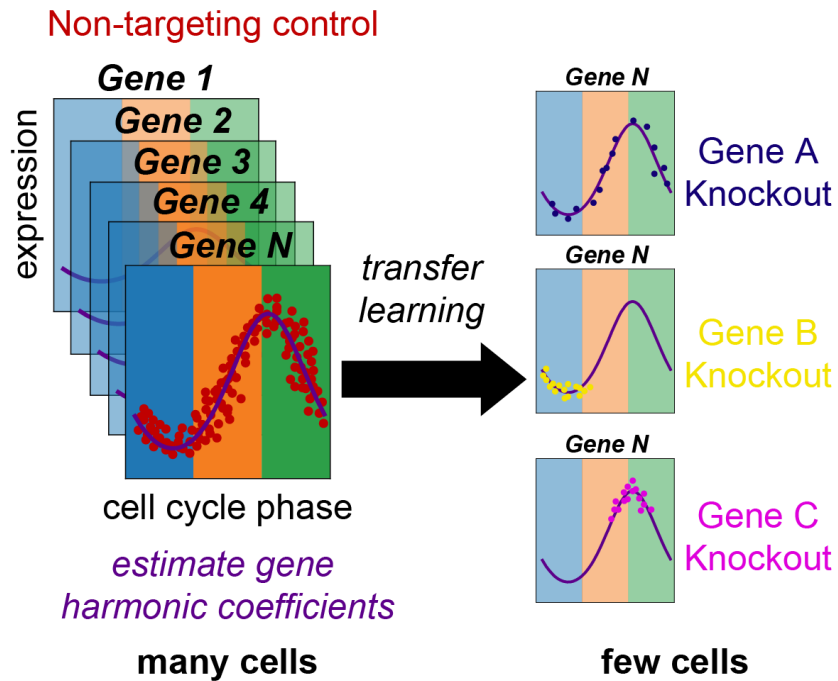
- Genome-wide Perturb-seq dataset in RPE1 cell line

# Transfer learning of gene harmonics enables study of the effects of gene knockdowns on velocity



**Transfer** gene harmonics inferred on non-targeted cells to obtain phases of **small batches** of knockdown cells

# Perturb-seq conditions with altered speed are linked to DNA replication, translation initiation, and mRNA splicing



167,119 cells from 986 knockdown conditions

# Takeaways

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- RNA velocity vector fields are inconsistent with the gene expression manifold.
- VeloCycle is a generative Bayesian model that couples velocity field and manifold estimation into a unified framework for periodic manifolds.
- VeloCycle can infer cell cycle periods on a real-time scale, validated by time-lapse microscopy imaging.
- VeloCycle can harness statistical testing and transfer learning in multiple *in vitro* and *in vivo* experimental contexts.